

Shock, Ballistic and Blast Properties of Granular Materials.

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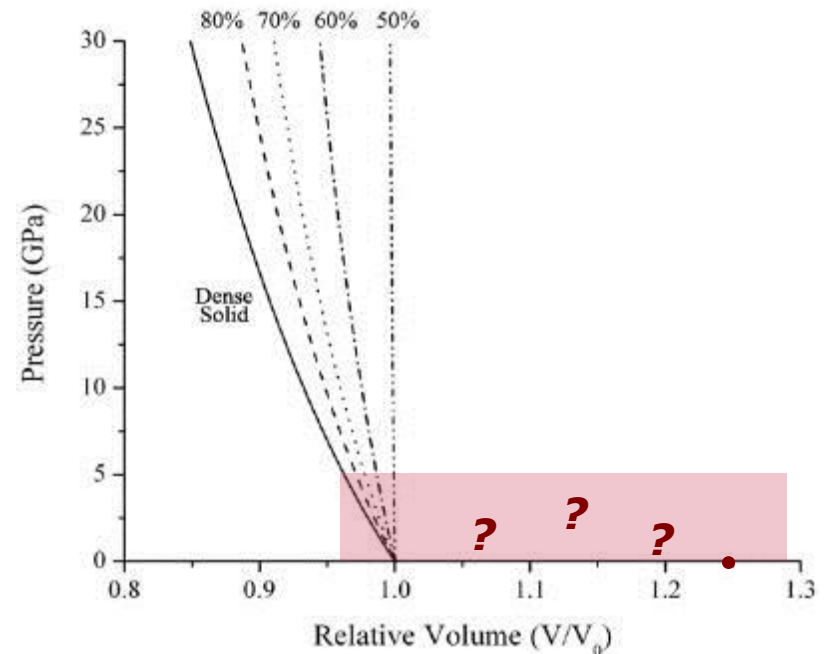
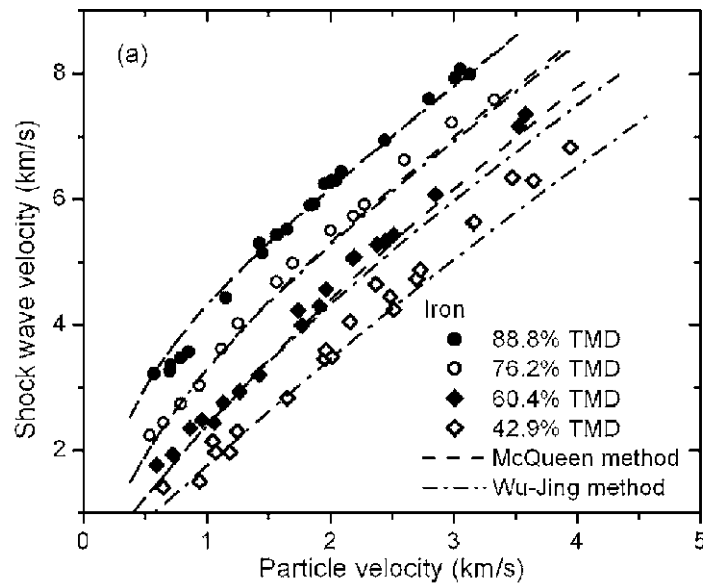
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Powders under shock loading

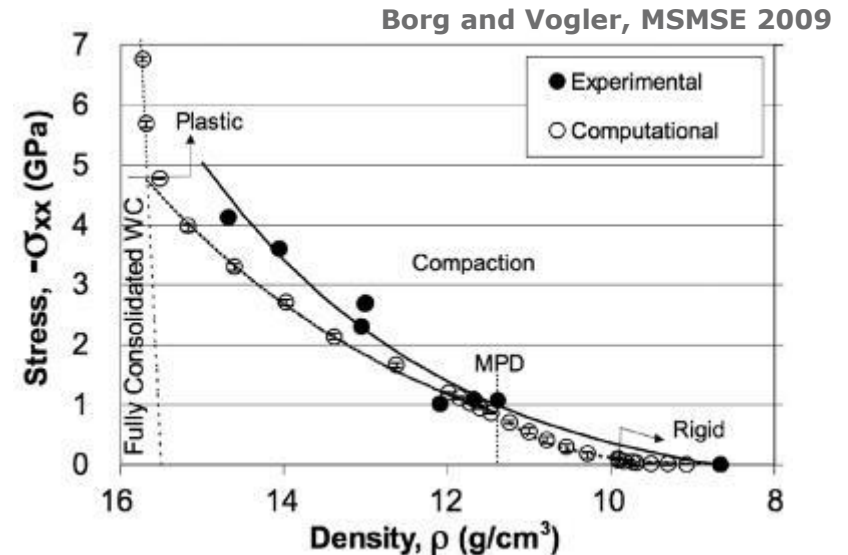
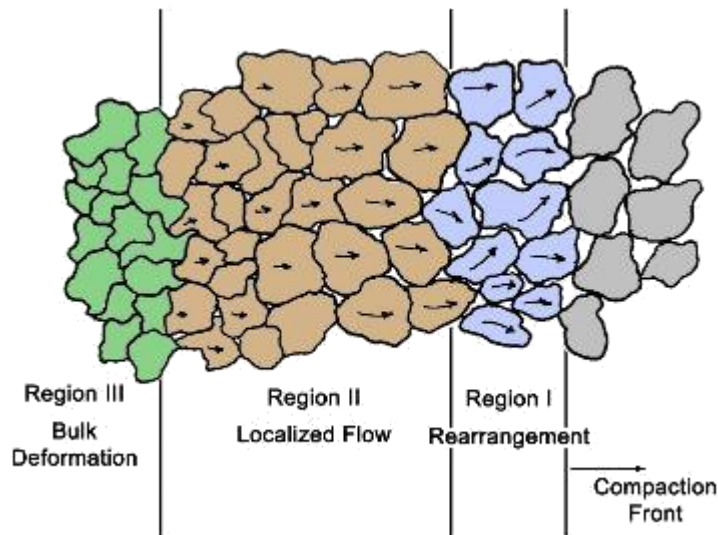
Response of powders to intense loading is reasonably mature

Porous models (McQueen, Wu-Jing, etc.) enjoy moderate success once significant void volume is eliminated



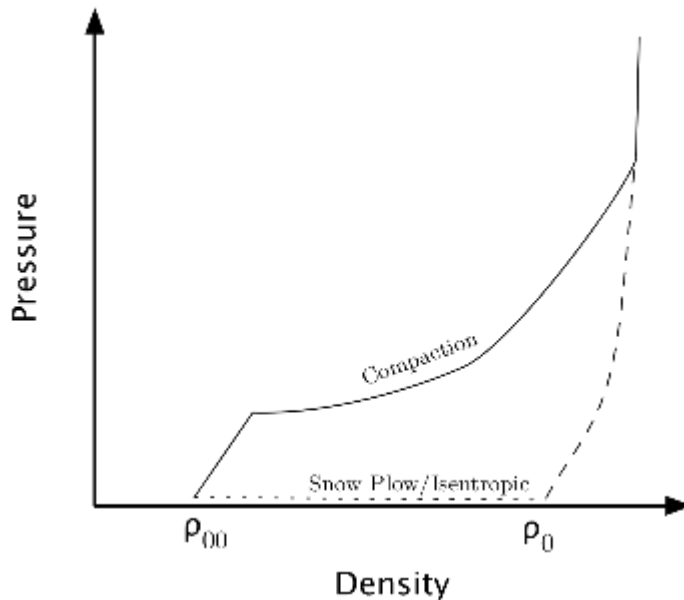
Densification process ignored

Densification at low stresses



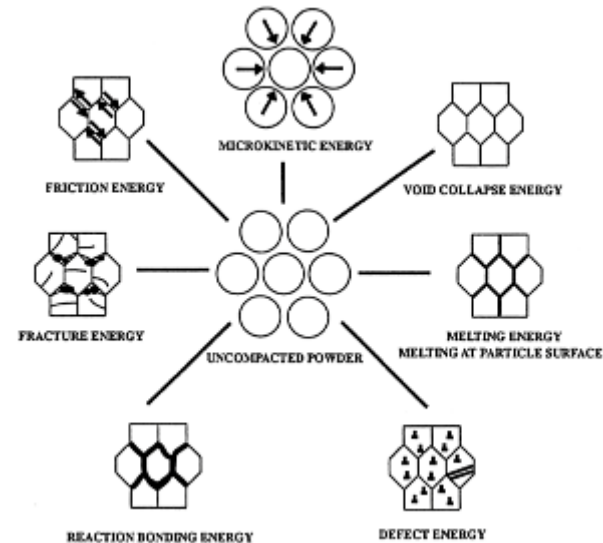
Several regions associated with the densification of granular materials under shock compression: rigid / compaction / bulk plastic

Models for compaction are generally exercises in curve-fitting, **insensitive to microstructure**



COMPACTION

- States with porosity.
- Significant energy absorption.
- Dominated by meso-structure of granular material.

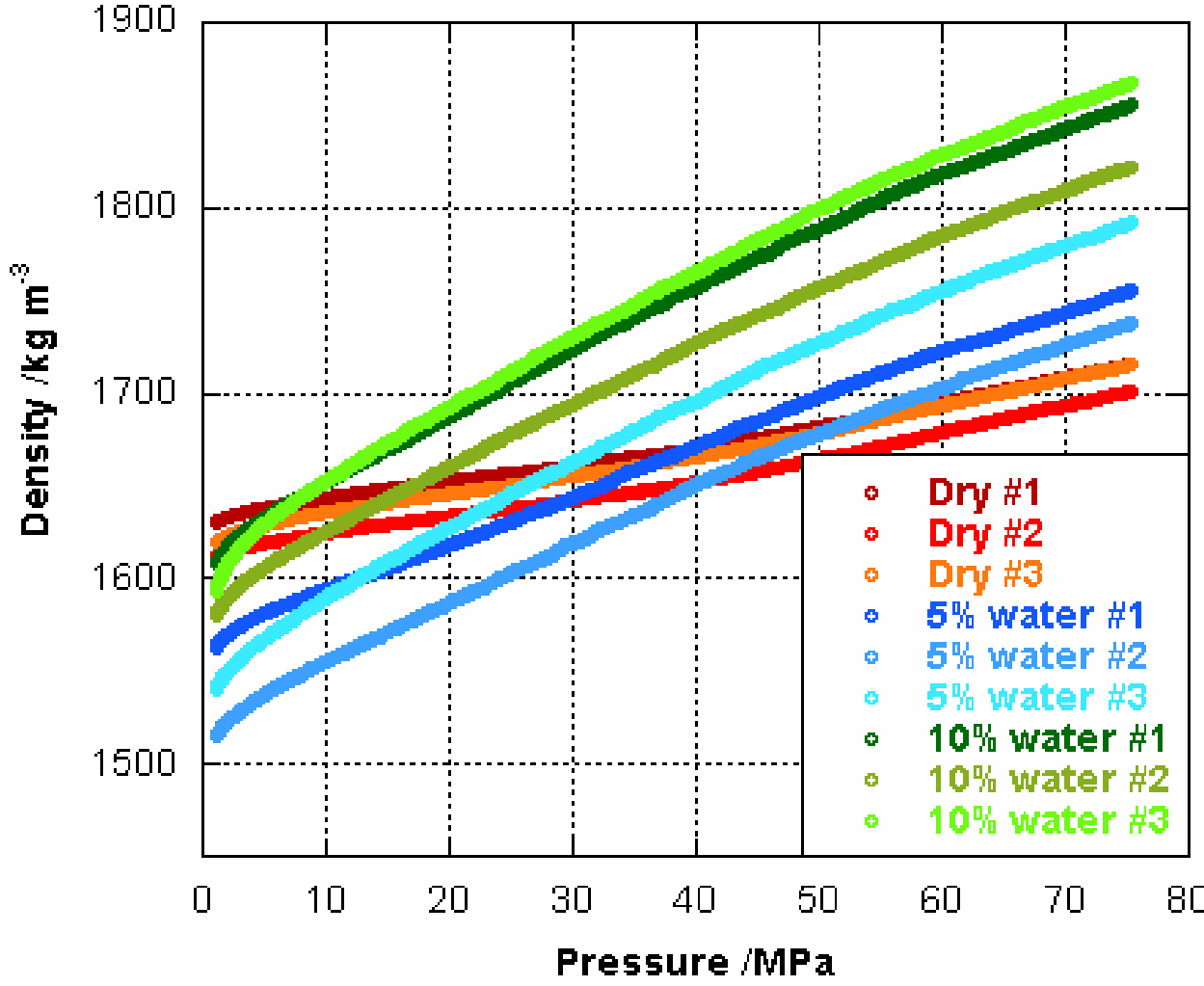


Meyers. Benson & Olevsky. Shock Consolidation: Microstructurally-Based Analysis and Computational Modeling. Acta mater 1999,

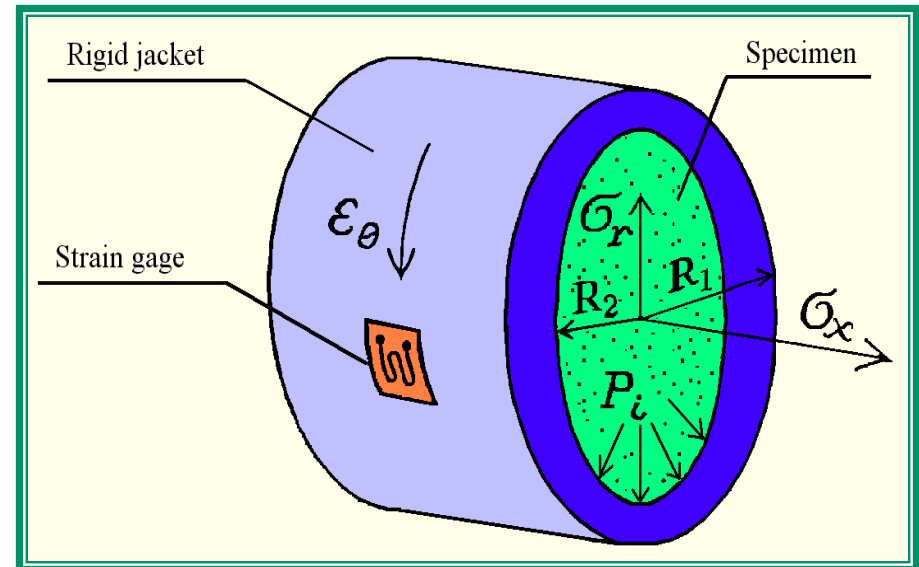
ENERGY DISSIPATION

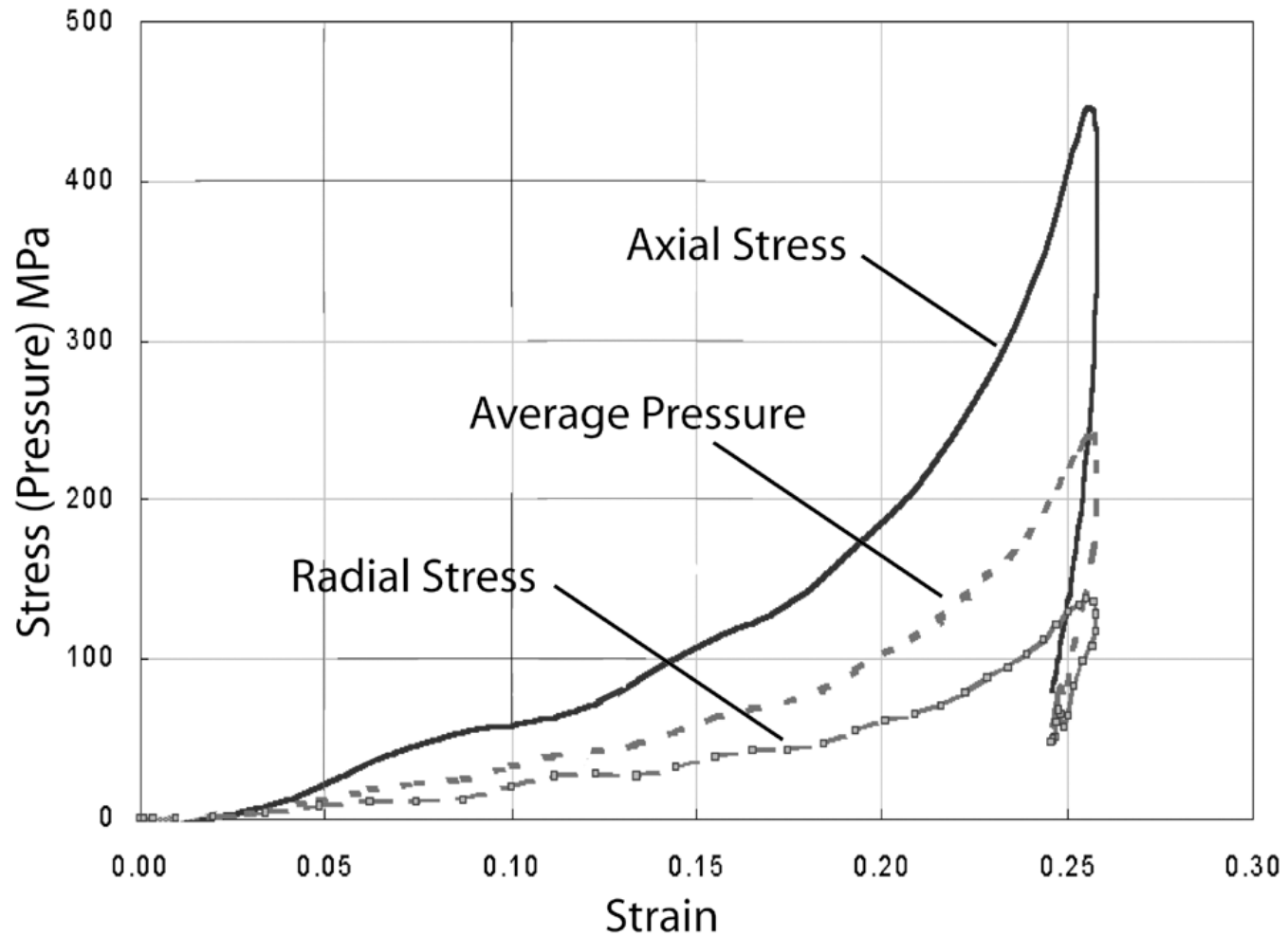
- Compaction energy associated with porosity removal.
- Quasi-static or dynamic – Benson et al. JAP 1997
 - Processes present in quasi-static compaction.
 - Processes ONLY in dynamic compaction.

Low-Rate : Moisture Content

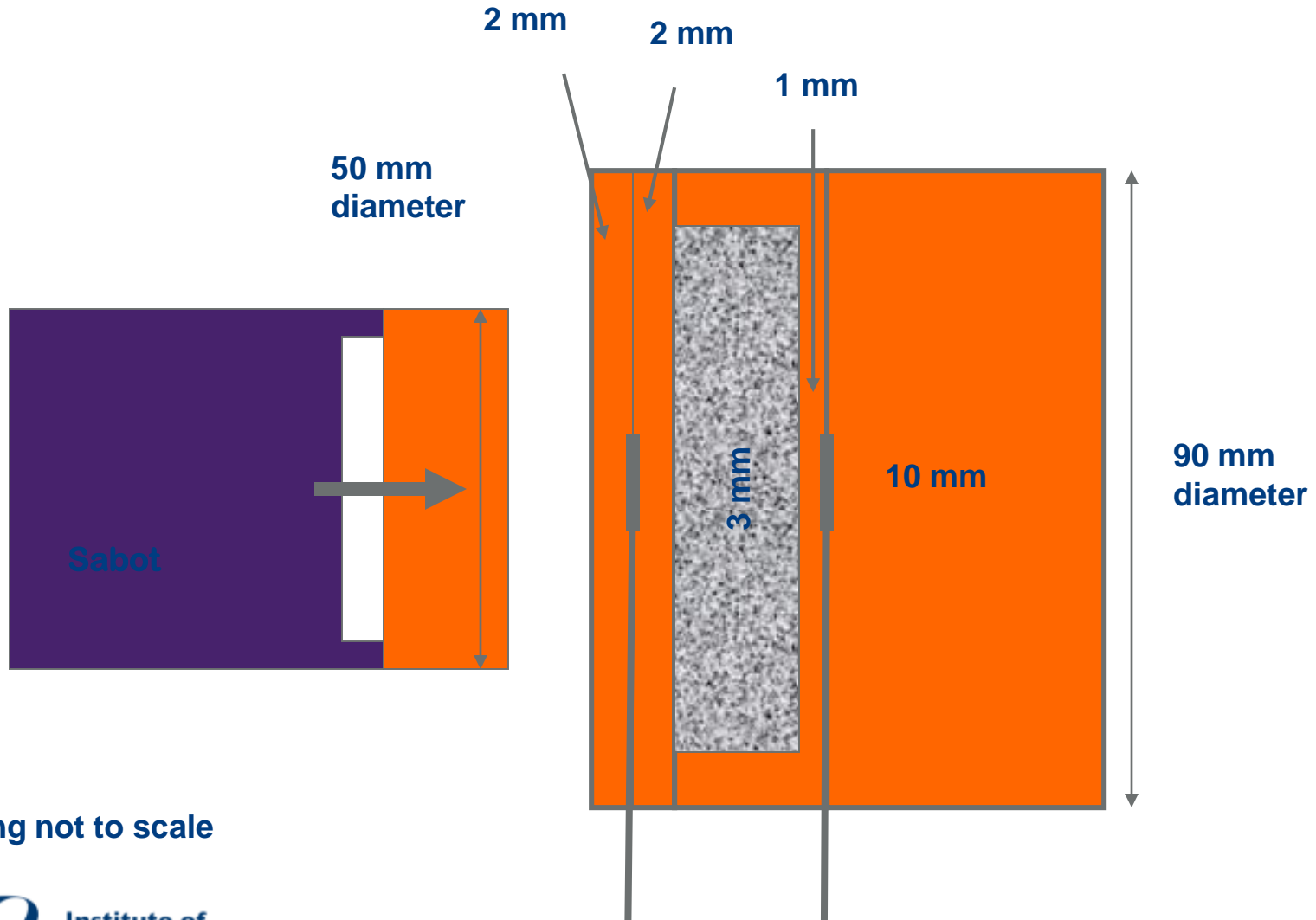


Stress components in a specimen and in the confined jacket



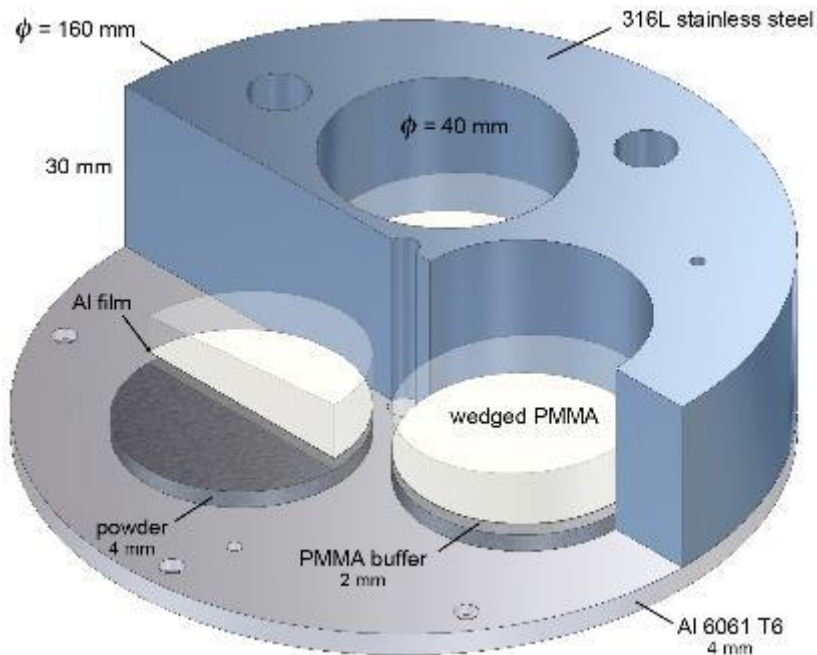


Sample Arrangement (High-stress)



Drawing not to scale

Plate-impact experiments



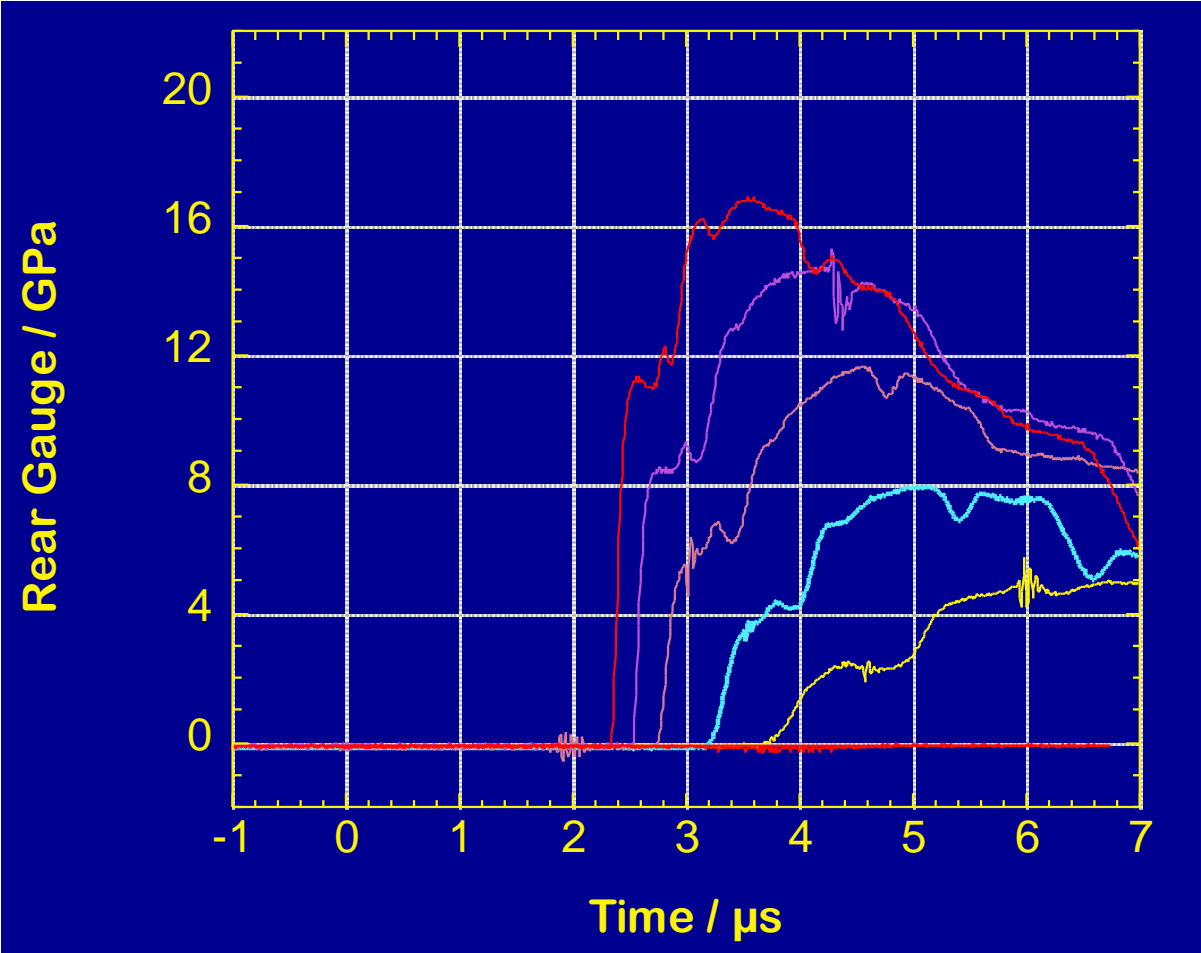
Multiple powder targets
subjected to identical
loading

8 HetV channels and two
pins to measure sabot
velocity, impact and
breakout tilt, and target
particle velocity

D. Eakins *et al.* SCCM 2011

Measured tilt < 2 mrad

Rear Gauge Variation



Rise time of first pulse

Shock velocity

200 m s⁻¹

- 1 μs rise time and U_s 1 mm μs⁻¹
- 1 mm or 4 grain particles

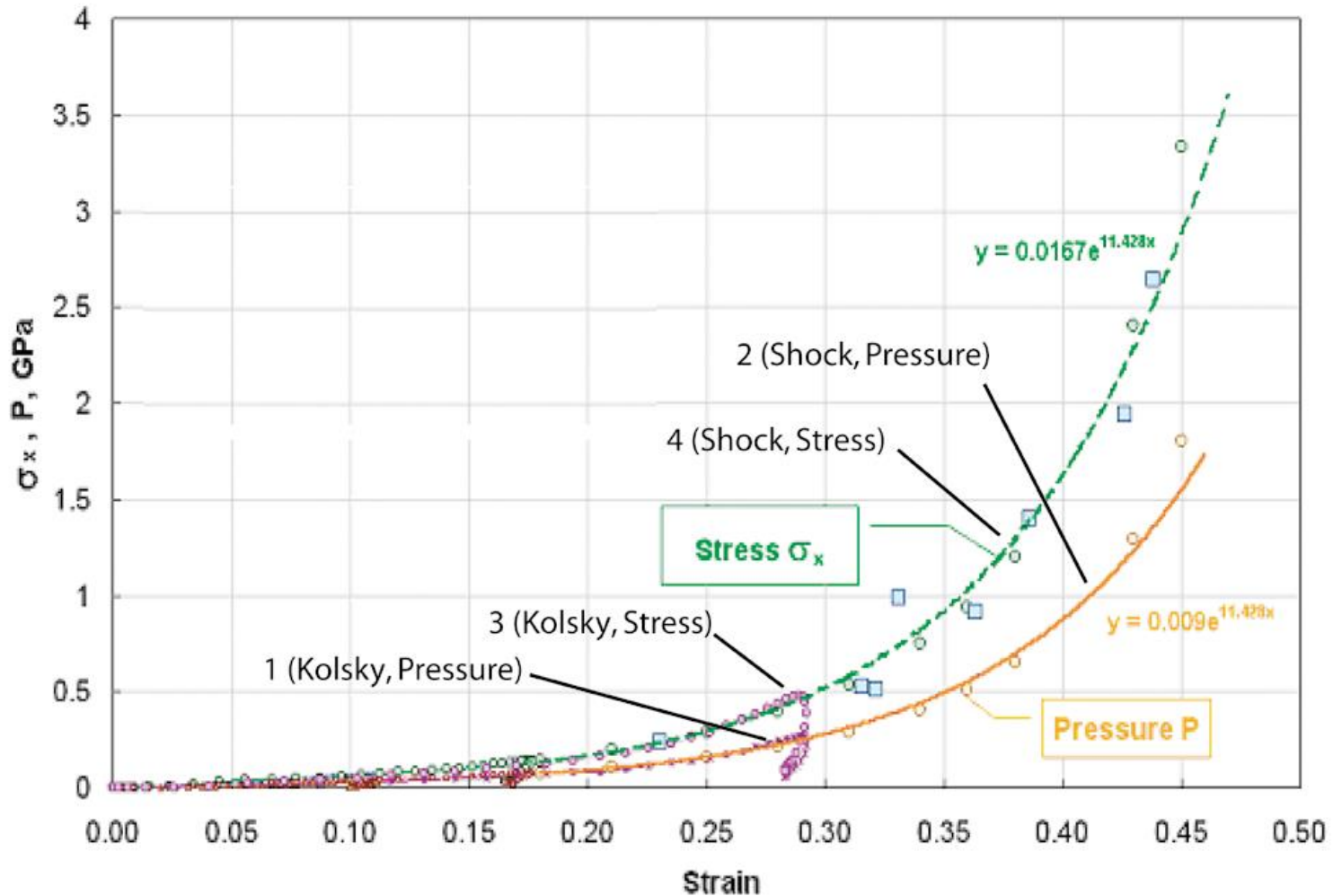
500 m s⁻¹

- 0.5 μs rise time U_s 1.4 mm μs⁻¹
- 0.7 mm or 3 grain particles

800 m s⁻¹

- 0.2 μs rise time and U_s 2 mm μs⁻¹
- 0.4 mm or 2 grain particles

Results Combined Stress + Pressure

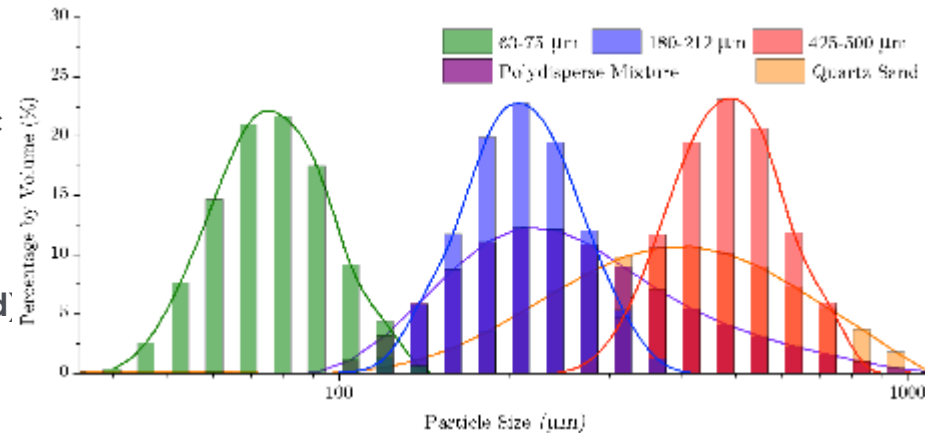


Initial Conclusions

- A given granular material compaction behaviour is self-consistent across the range of strain rates
- Probably due to the system being able to move from one compaction process to another in a ‘smooth’ fashion.
- Quantitative prediction of the compaction process is difficult and often a case of post-experiment curve fitting.
- **However – this is very much a first-order approximation!**
- So can we look at some aspects in more detail?

SAMPLE MATERIALS

- Soda-lime glass microspheres – Whitehouse Scientific
 - 3X monodisperse distributions
 - 1X polydisperse distribution
- Quartz Sand – Eglin Air Force Base, Florida (Eglin Sand)

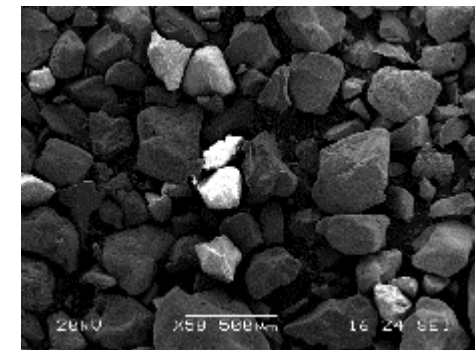
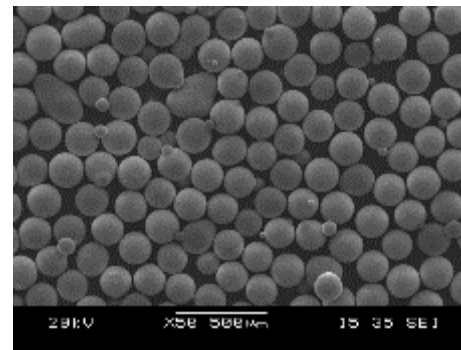


PARTICLE SIZE ANALYSIS

- Malvern Mastersizer laser diffraction particle size analyser.
- Narrow distributions

SCANNING ELECTRON MICROSCOPY (SEM)

- Spherical particles
- Some surface flaws.



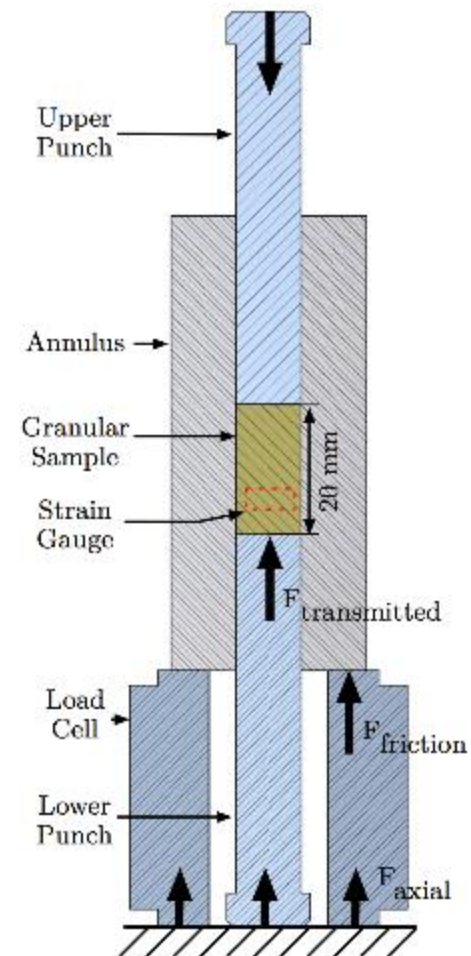
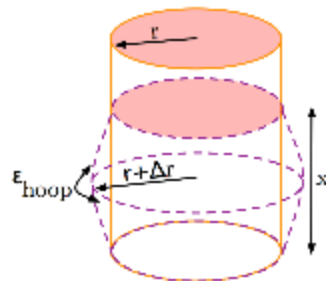
Quasi-static Compaction Experiments

AIM

- Determine quasistatic response to easily analyse morphology changes within bed.

METHOD

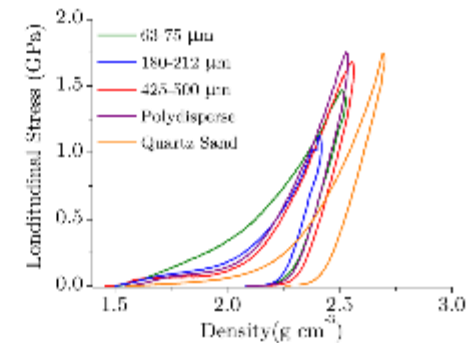
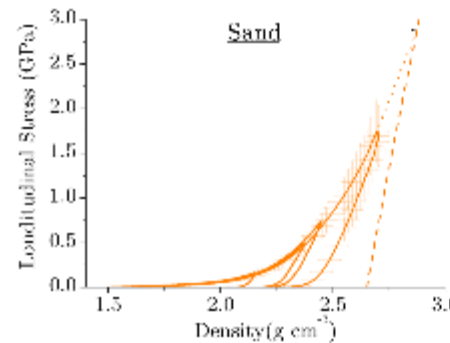
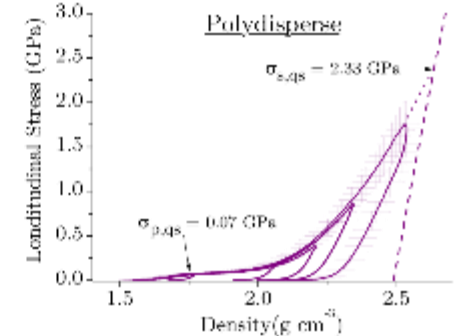
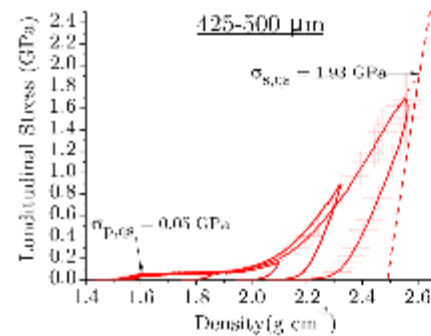
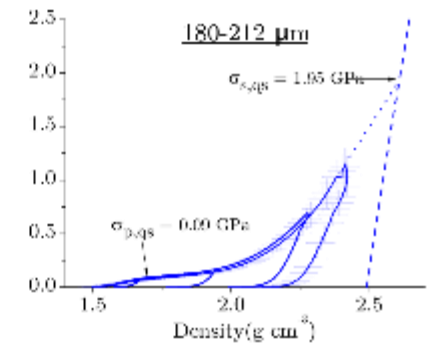
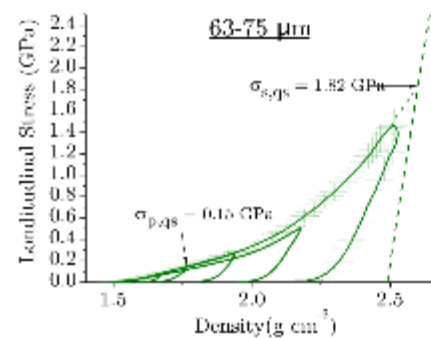
- Wall friction effects reduced and removed.
- Sample volume calculated through displacement and annulus strain measurements.



Stress-Density Response

RESULTS

- Microsphere samples showed transition in loading curve indicating increasing strength with decreasing particle size (σ_p).
- More energy absorbed during compaction with smaller particles.
- No measurable transition in sand samples ($\sigma_p=0$).
- No trend in stress required to achieve full compaction (σ_p)
- Porosity was present in all compacted samples.



Post Loading Analysis

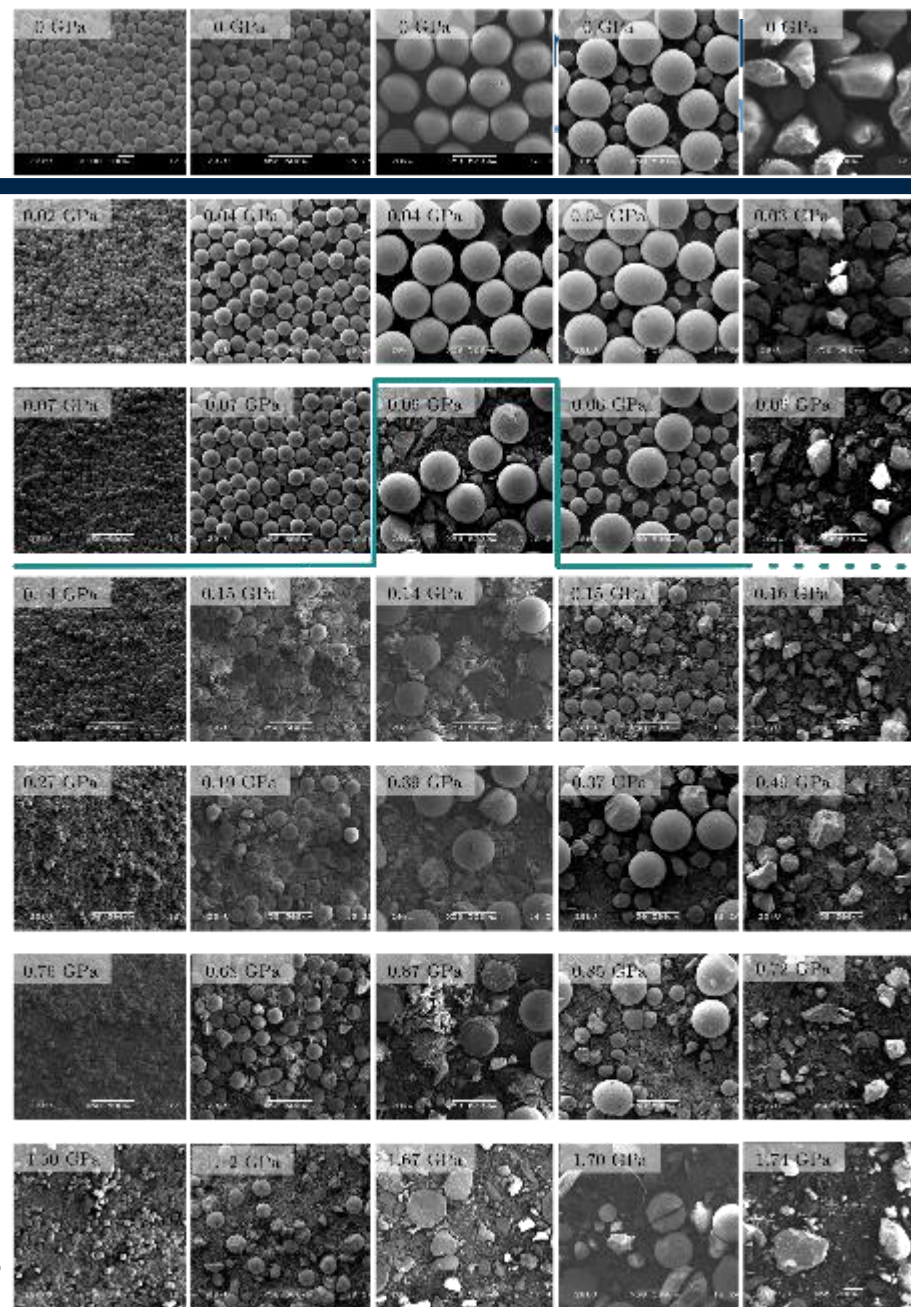
SPHERES

- No fracture seen in stresses below σ_p .
- Fracture initiates at σ_p
- Large amount of whole spheres beyond σ_p .

SAND PARTICLES

- Constant fracture even at minute loads.
- Difficult to determine which particles fractured

Longitudinal Stress

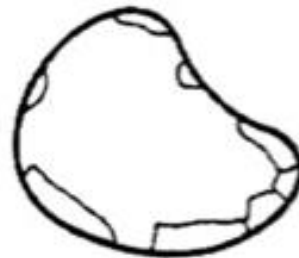


63-75 μm 180-212 μm 425-500 μm Polydisperse Quartz Sand



Abrasion:

Granulometry remains almost constant but with a production of fine particles



Attrition:

Grain breaks into one grain of a slightly smaller size and several much smaller ones



Fracture:

Grain breaks into smaller grains of similar sizes

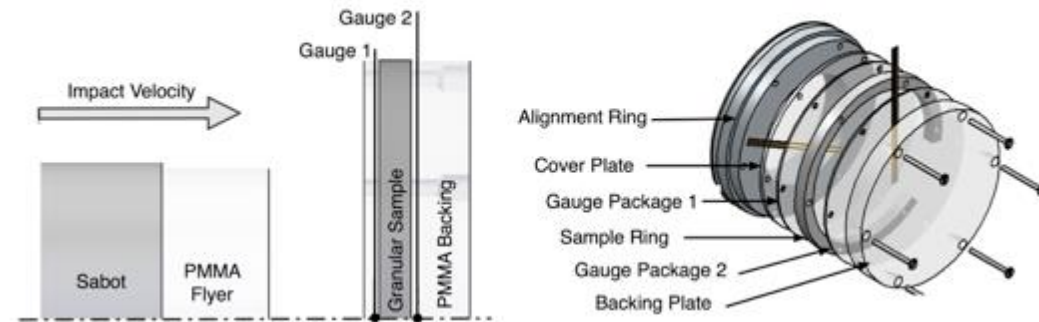
Shock Compaction Experiments

PLATE IMPACT TESTING

- 50 mm Single stage light gas gun
- 200 – 1000 ms⁻¹ PMMA and Cu flyers
- Velocity: $\pm 1\%$
- Alignment: ± 2 mrad

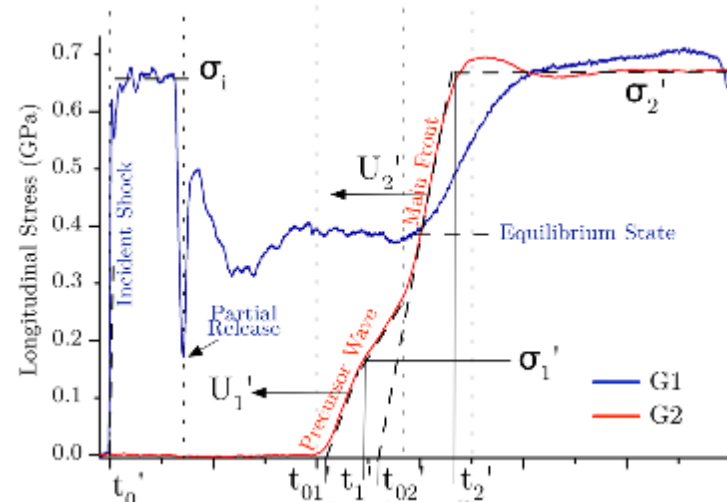
CELL DESIGN

- PMMA encapsulation
 - » Impedance match to epoxy resin
 - » No “ring up” in gauges
 - » $\pm 4\mu\text{m}$ parallel
- Longitudinal stress gauges (LM-SS-125CH- 048)



MANGANIN LONGITUDINAL STRESS GAUGES

- Piezo-resistive response to longitudinal stress
- Macro-scale measurement.
- 14.15 mm² active gauge area.



Precursor

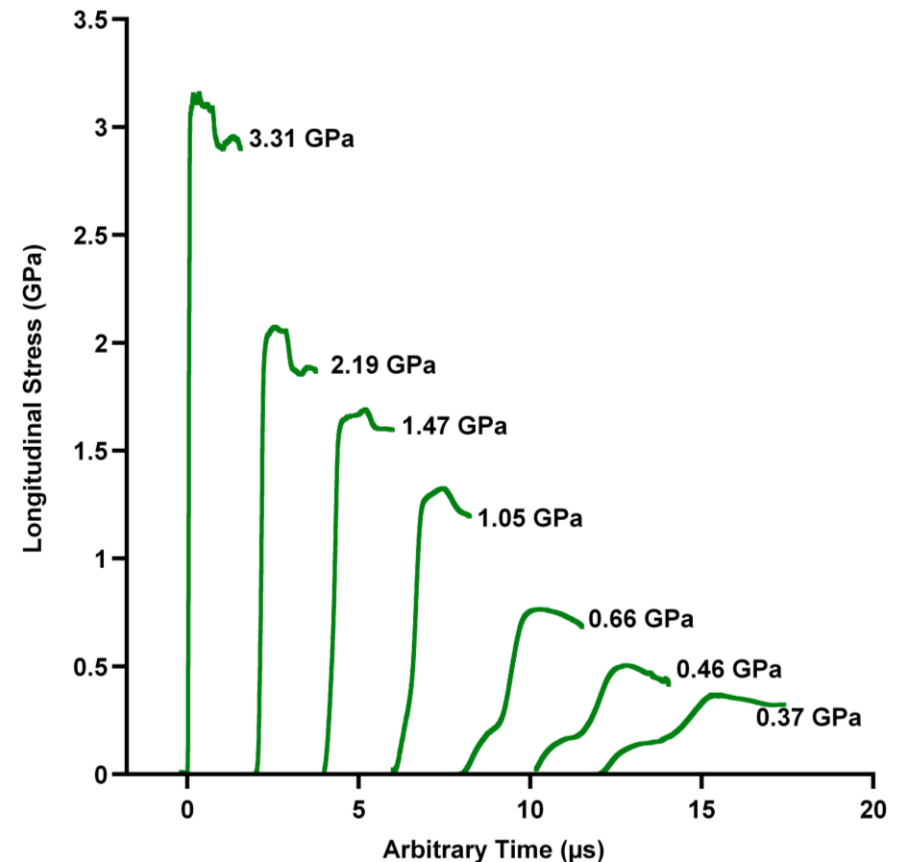
- Constant Stress
- Particle Rearrangement? *
- Decays with Input Stress

Shock

- Rise time decreases

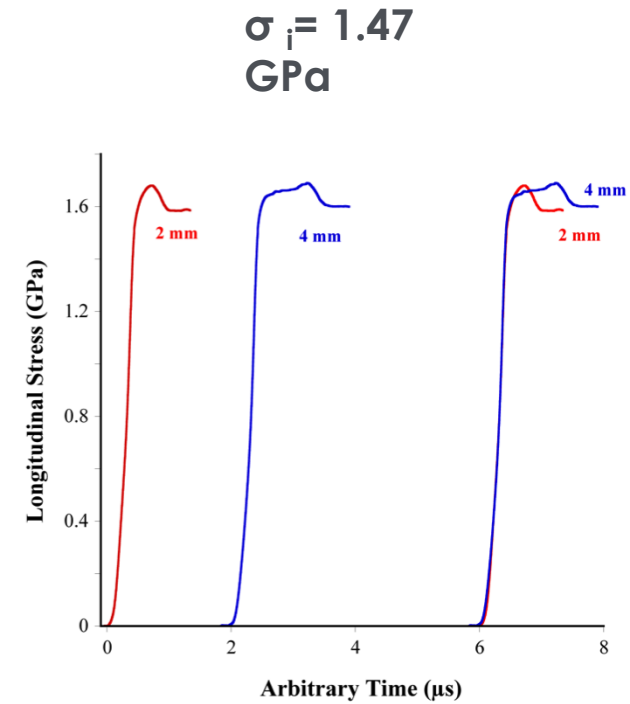
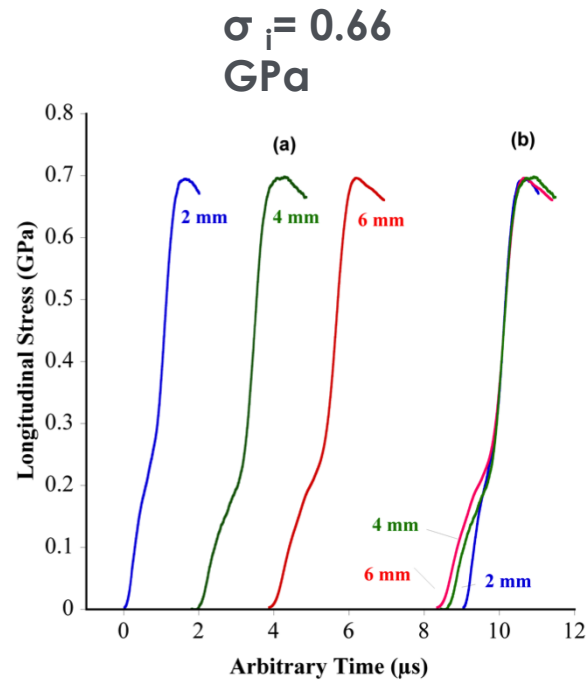
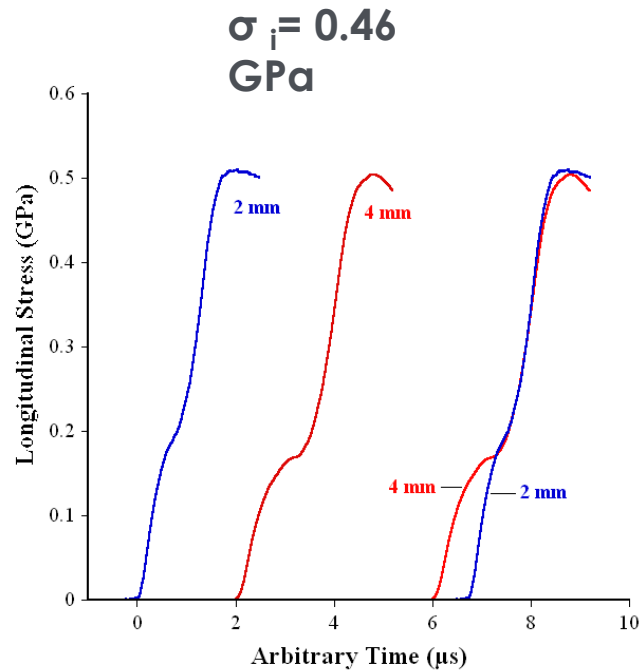
Overshoot

- Proportional to bed thickness
- “Partial release due to particle fracture”*



*Tsembeis et al, 2002

Precursor Evolution – Bed Thickness



Particle Size Effects

Prior Understanding

- Hugoniot is not affected by particle size (metal powders*)
- Shock-wave thickness is proportional to particle size (metal powders*)

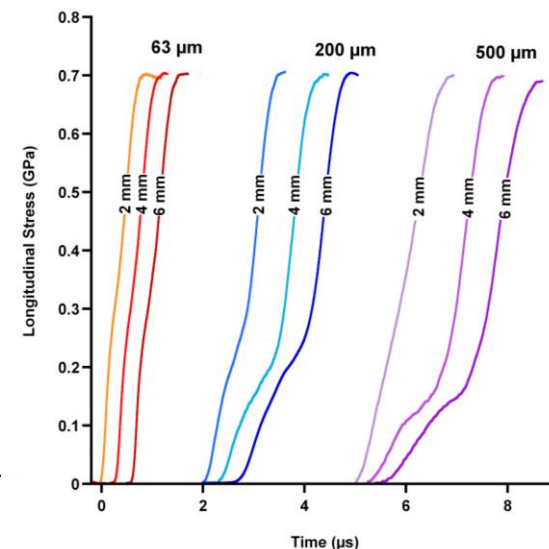
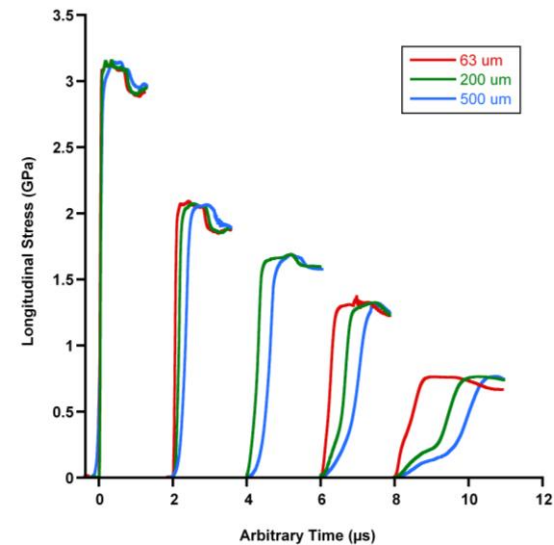
Current Conclusions

- Shock thickness is affected by particle size (mono-disperse) or some length scale
- Clear difference in shock TOA (U_s)

Ongoing Investigation

- Bi-dispersity
- Reduced porosity
- Particle size or pore size dependent

*Nesterenko, 2001



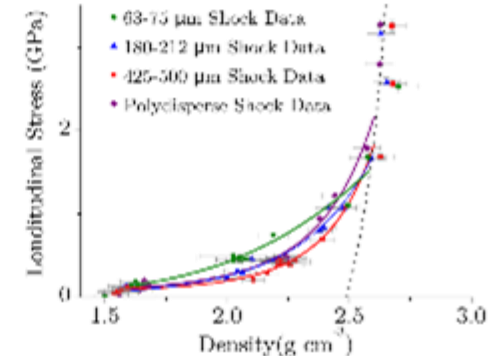
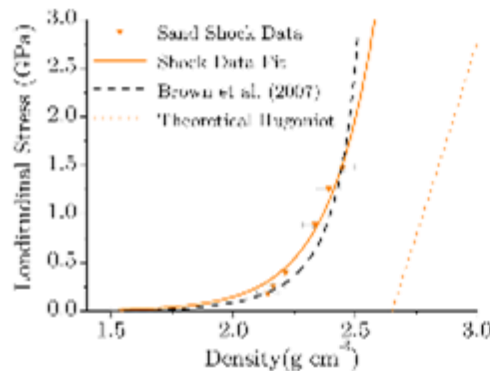
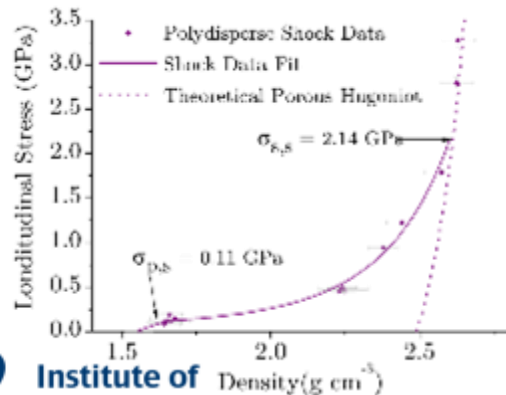
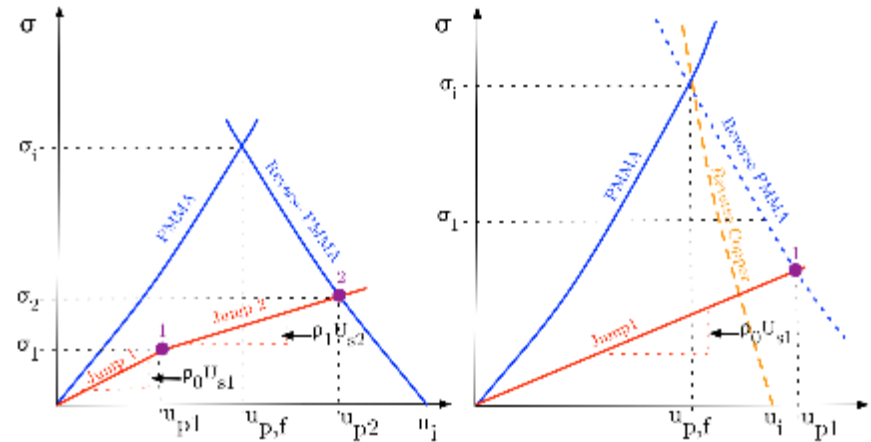
Shock Compaction Curves

ANALYSIS PROCESS

- Linear fits to transmitted wave profiles.
- Wave velocity measured and jumps applied to infer densification.
- Relatively insensitive to wave magnitude

COMPACTION CURVES

- Precursor wave inferred initial jump.
- Magnitude increased with decreasing particle size.
- Microsphere curves intersected porous Hugoniot.
- No measurable precursor wave in sand.



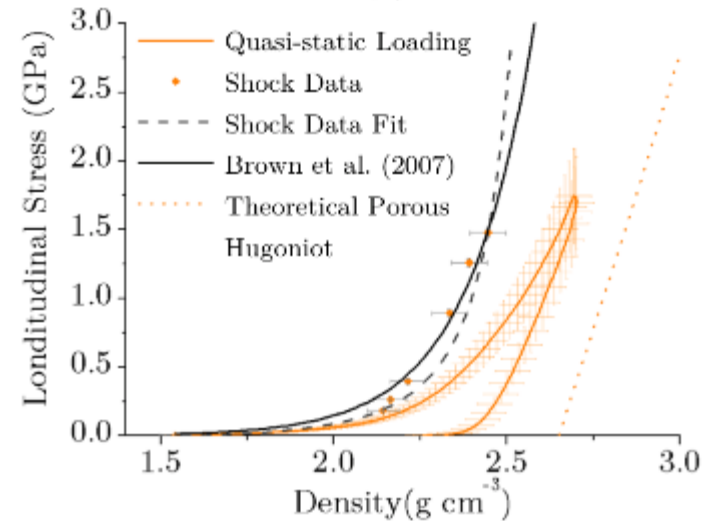
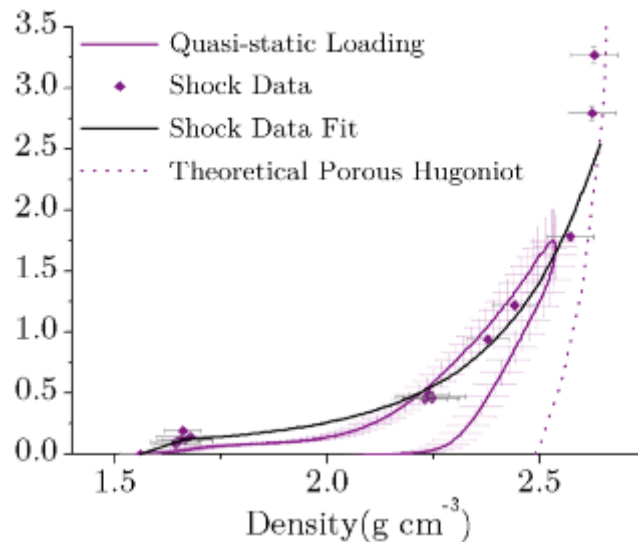
Comparison Between the Strain Rates

SPHERES

- Shock compaction curves agree with quasi-static curves.
- Initial strength of beds higher in shock compaction regime. More particle fracture?

SAND

- Curves do not agree.



Conclusions (Compaction)

The compaction response is affected by particle size.

Beds of smaller particles have an increased macro-scale strength due to a likely increase in load carrying contacts at a boundary despite a reduced particle strength.

The compaction wave profile affected by particle size

The wave duration and features are dominated by particle size. The particle-elastic-limit of a bed produces a precursor feature.

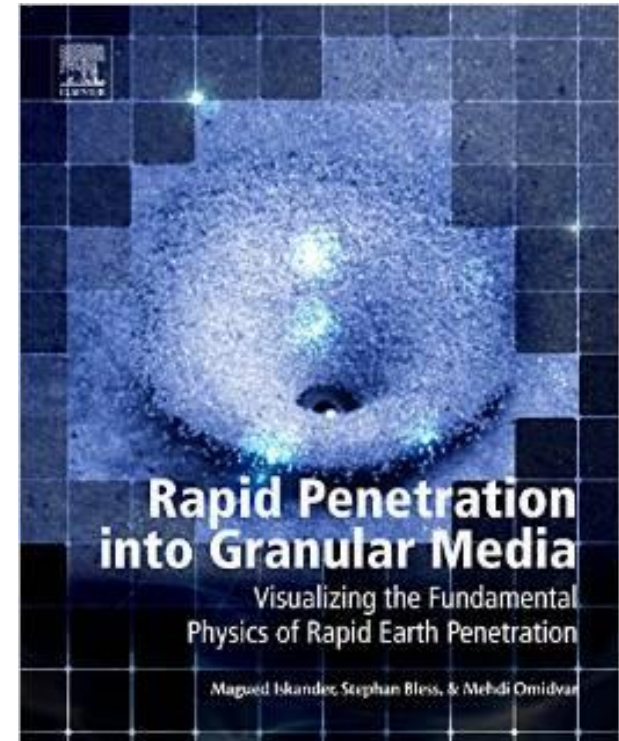
Compaction of Brittle granular materials

There are fracture dominated processes that are controlled by particle morphology. Beds of regularly shaped particles favoured an energy expensive total-fracture mechanism while irregular shaped particles abraded and rearranged thus consuming far less energy.

Quasi-static versus Dynamic processes

There was agreement with the low and high strain-rate loading data for spherical glass particles. The quartz sand data indicates there was a significant contribution from dynamic-only processes.

Ballistic Experiments (2001 onwards)



The use of digital speckle radiography to investigate the internal flow fields during the ballistic penetration of sand

J.W. Addiss , A.L. Collins , S.M. Walley*, W.G. Proud (2015)

Sand Experiments

Digital Speckle Radiography

Digital Image Correlation

Flash X-rays

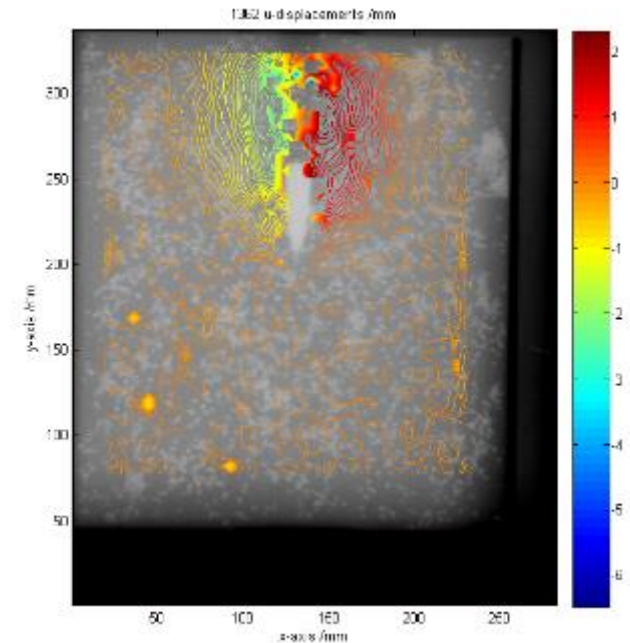
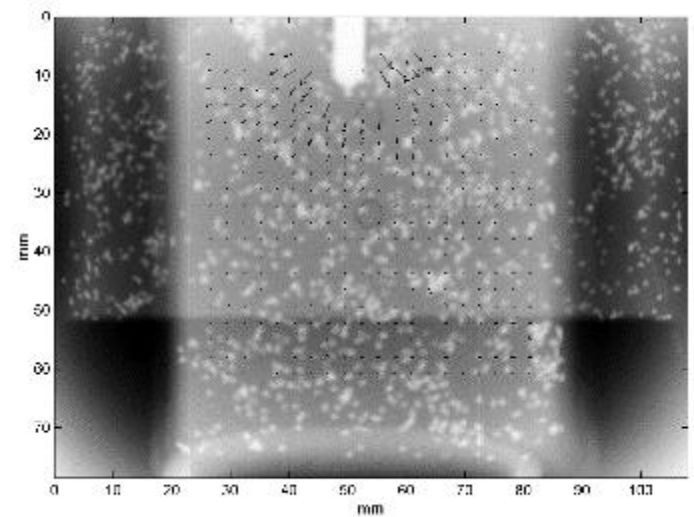
Embedded Particles

300 μm to 600 μm sand grains

60 \times 70 \times 30 mm^3 PMMA container

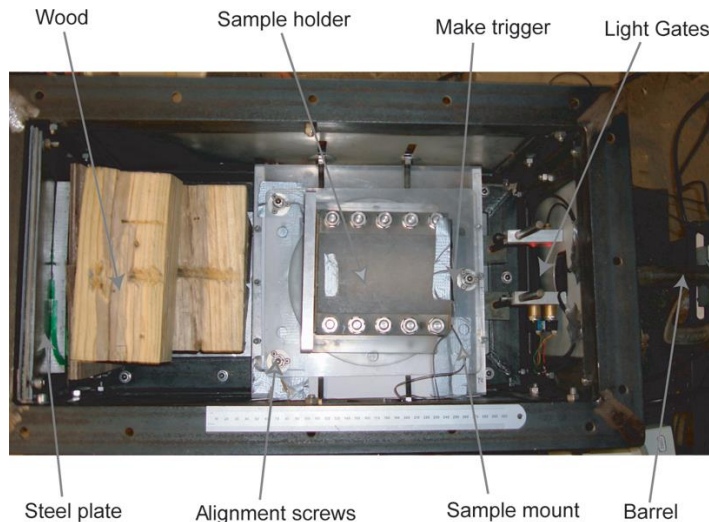
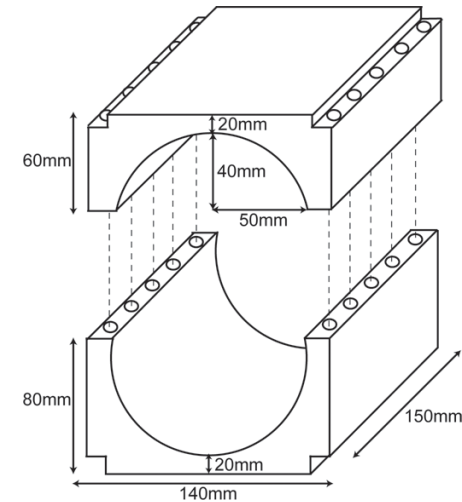
30 mm depth of sand

Copper rods 50 mm \times 5.0 mm \varnothing , mass 8 g, $v \approx 100 \text{ ms}^{-1}$



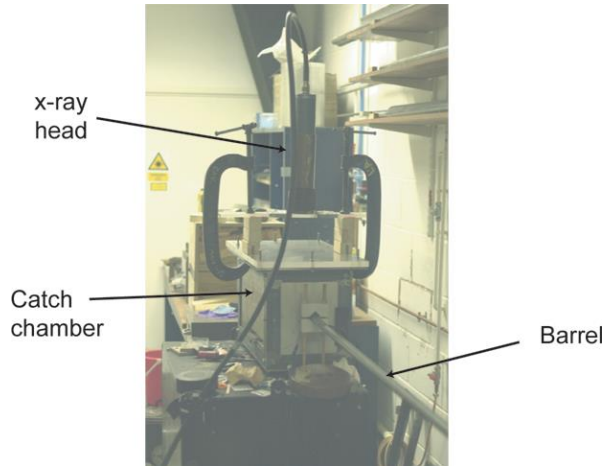
Experimental Setup

- **Cylindrical sample of sand, 150 mm long and 100 mm diameter.**
- **Horizontal layer of randomly scattered lead pieces running along the length of the cylinder (in the central plane)**



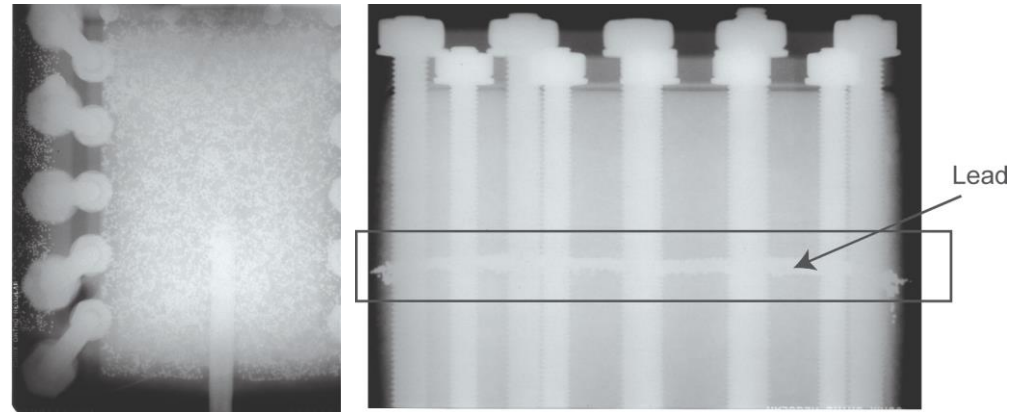
- **Projectiles launched at 200 m/s using a light gas gun**
- **10 mm diameter, 100 mm length, 55g and flat ended**

Experimental Setup

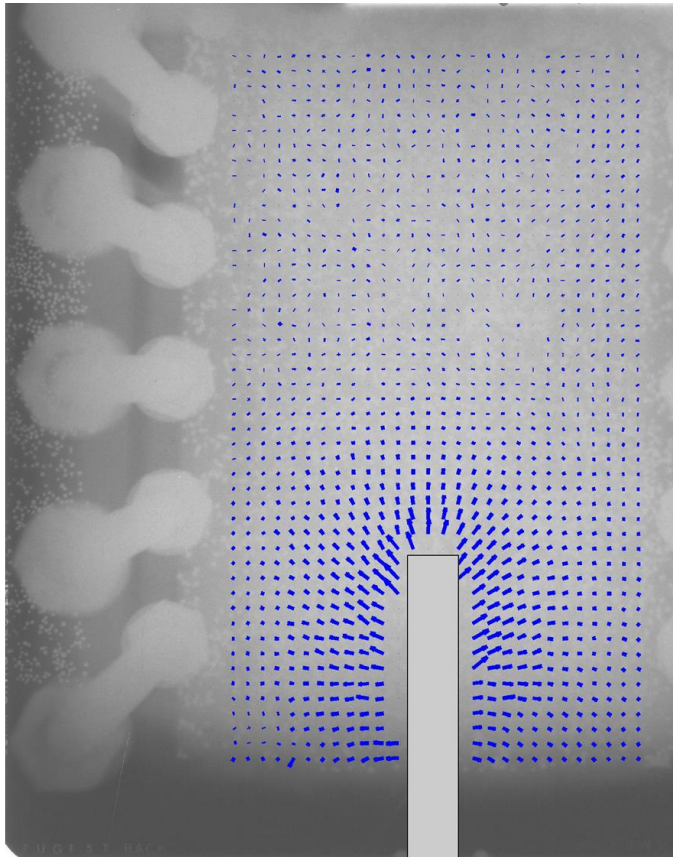


- Flash x-ray head mounted above sample used to take x-rays before and during penetration
- Series of experiments carried out to build up a sequence of images showing the penetration

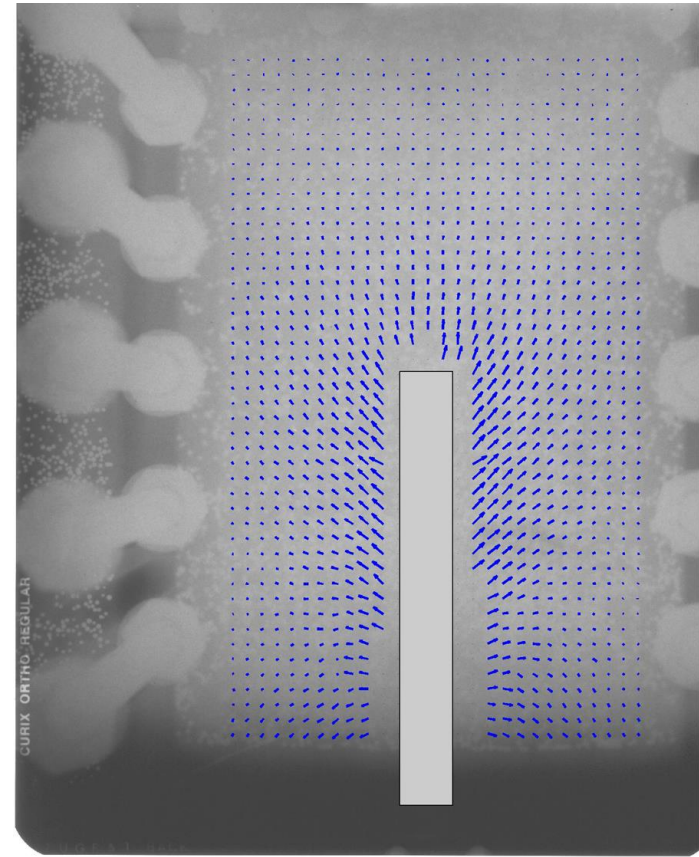
- X-ray images analysed with a DIC algorithm to calculate displacements



Measured Displacements

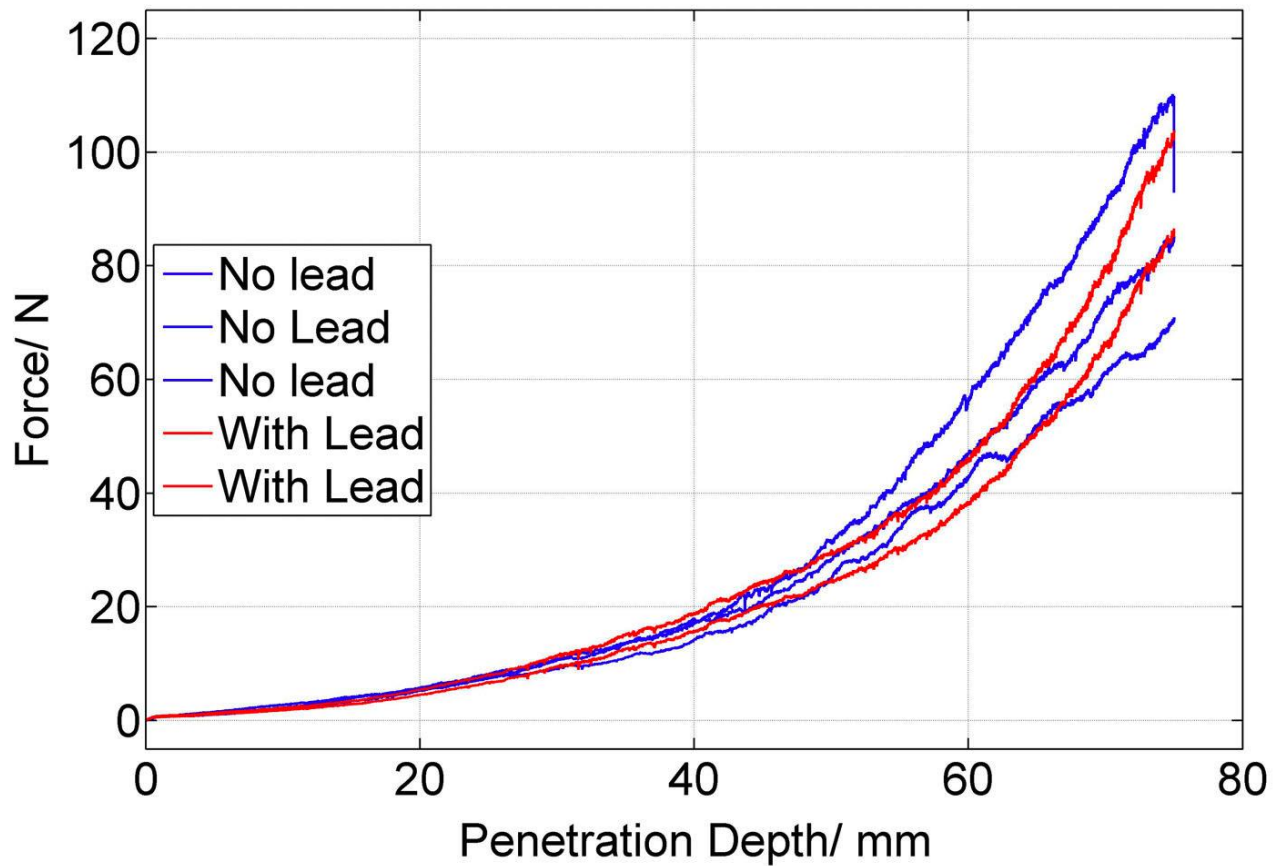


250us after impact

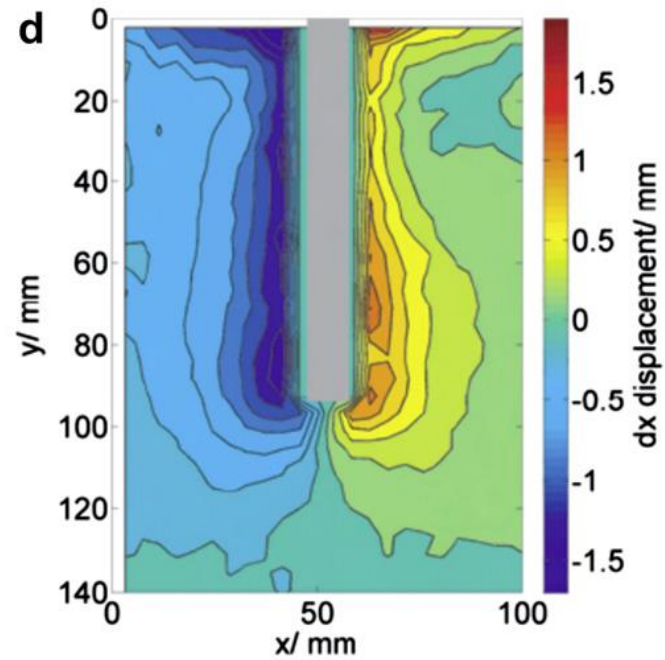
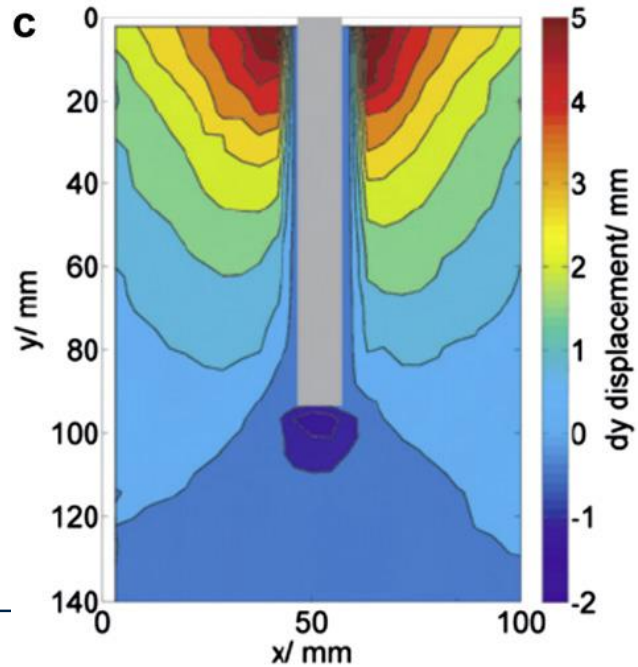
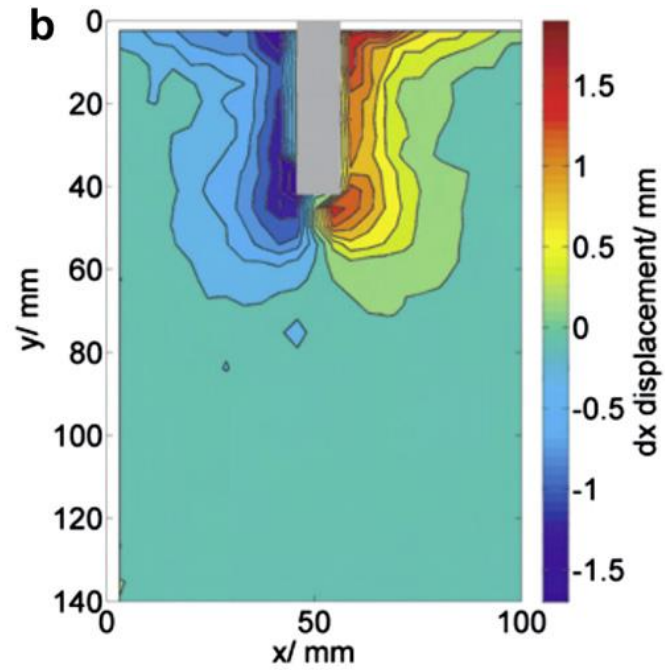
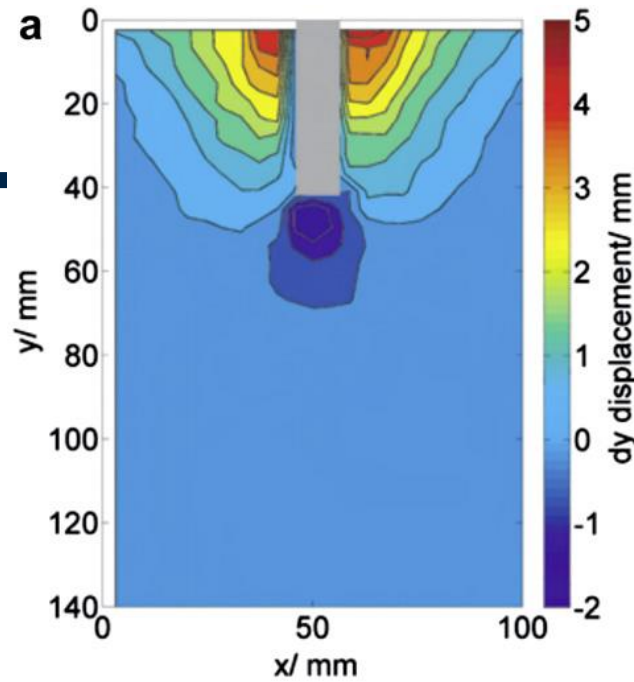


450us after impact

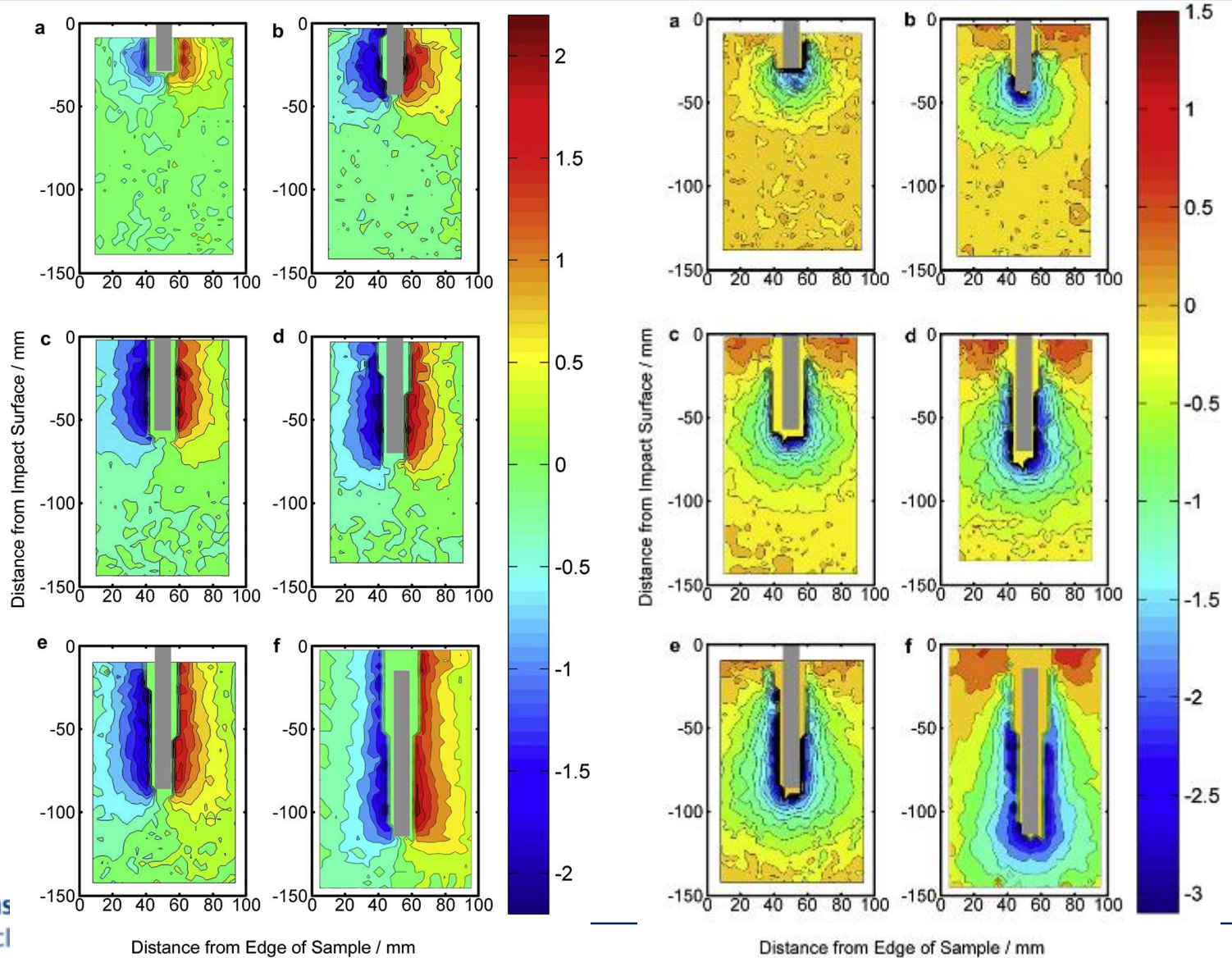
Comparison – with and without lead layer



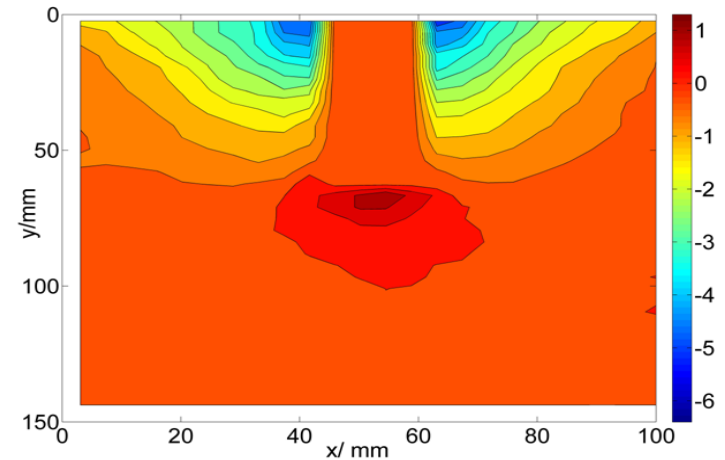
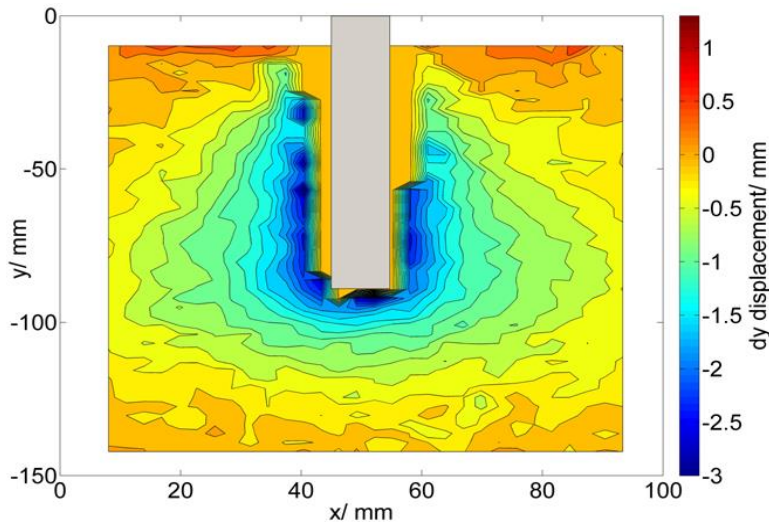
Low Rate Penetration 1.5 mm/min



Dynamic Penetration (200 m s⁻¹)



Comparison – Quasi-Static to Dynamic



- In the quasi-static case most of the material down to the rod tip is moving upwards
- There is no travelling compaction wave in the material

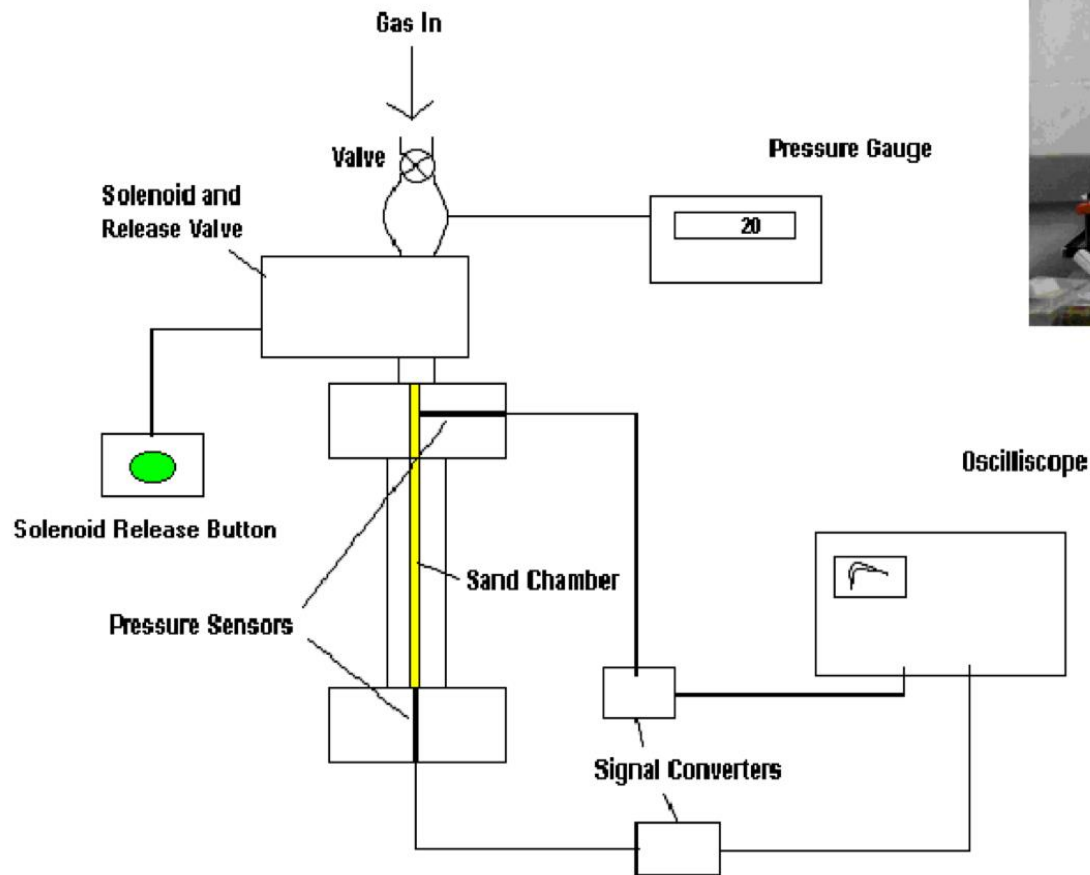
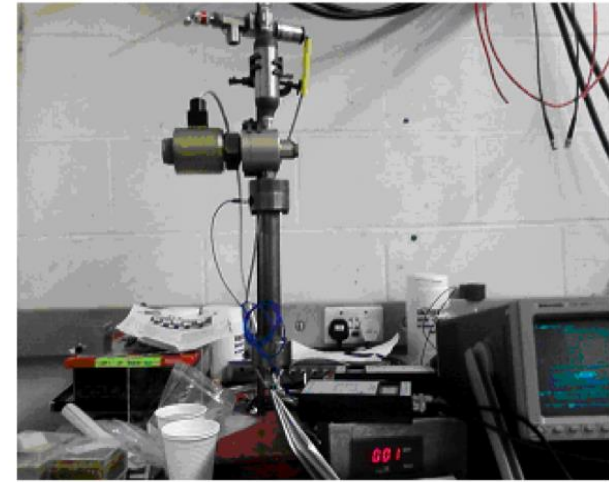
Conclusions (Ballistic)

- The higher the impact velocity (strain rate) – the smaller the volume of the granular material involved.
- There is a definite compaction wave in the higher rate systems
- Particle motion dominates at lower rates
- Particle rotation – occurs but is not measured in these experiments

Blast Response (SCCM 2013)

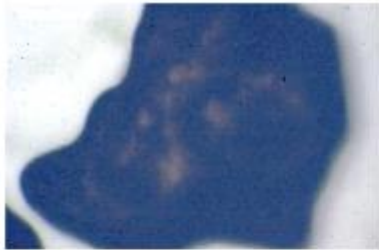


**Acknowledgement: David Johnson/Ray
Flaxman/Bob Marrah/Matthew Leal & Ian Hewitt**

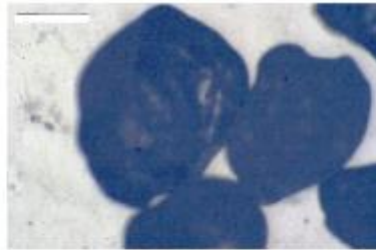


**Sand Column
6mm diameter
210 mm long**

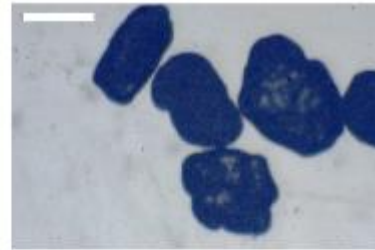
Sands used



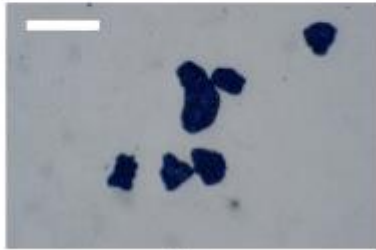
A



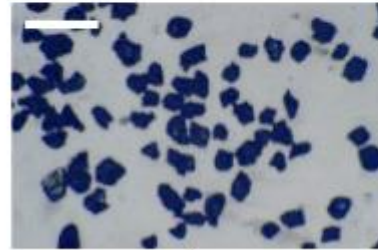
B



C



D

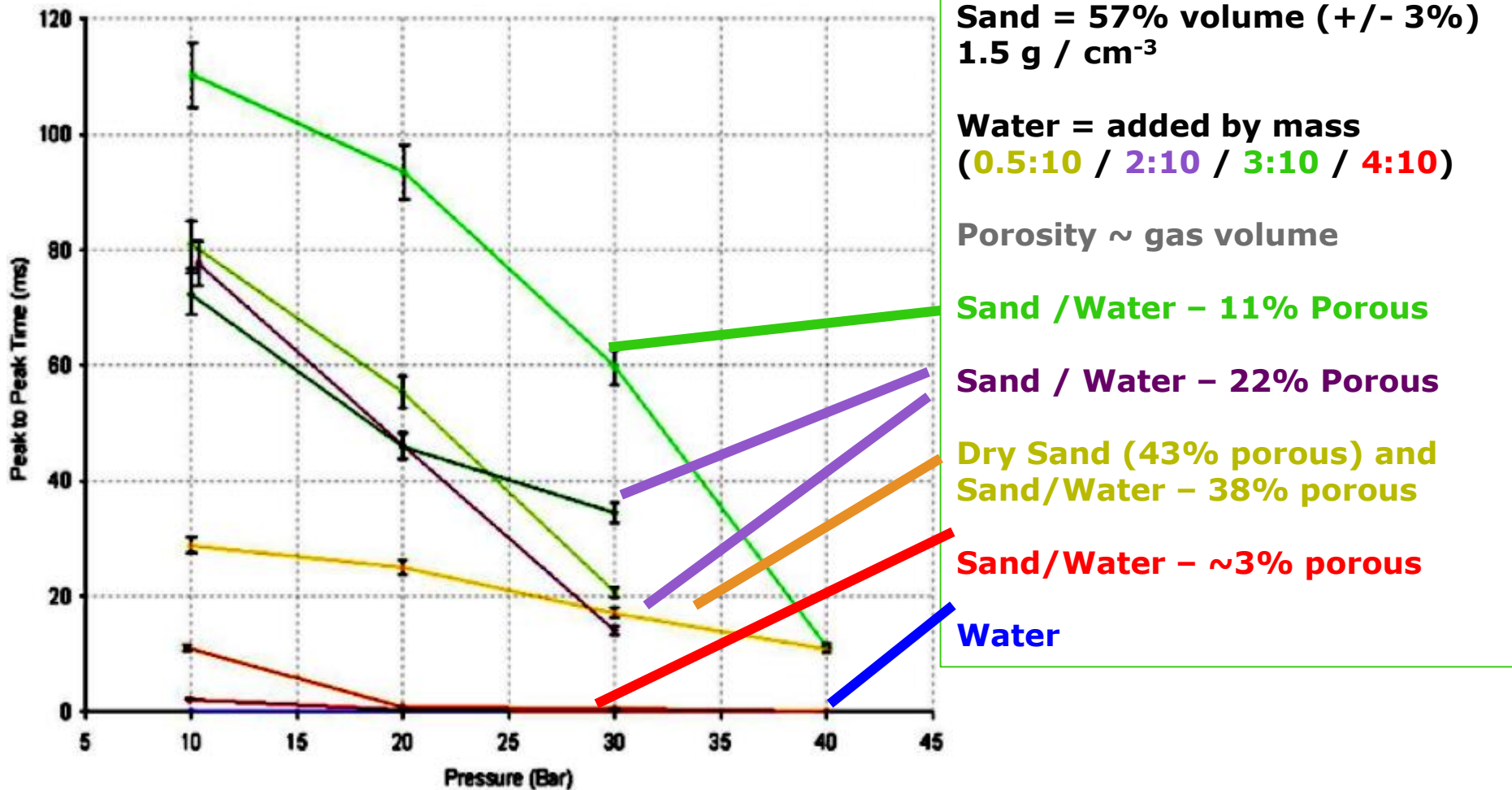


E

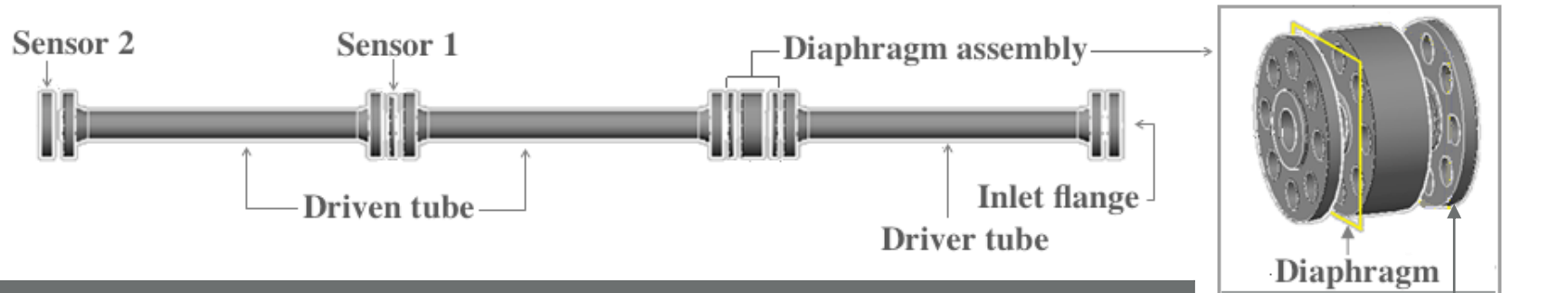
**Quartz Sand
dry = 43% porous
(all sizes)**

<u>Sand Size Type</u>	<u>Size - Manufacturers Specification (μm)</u>
A	1180-2360
B	600-1180
C	300-600
D	150-300
E	90-150

Peak to Peak Effect of Water Content

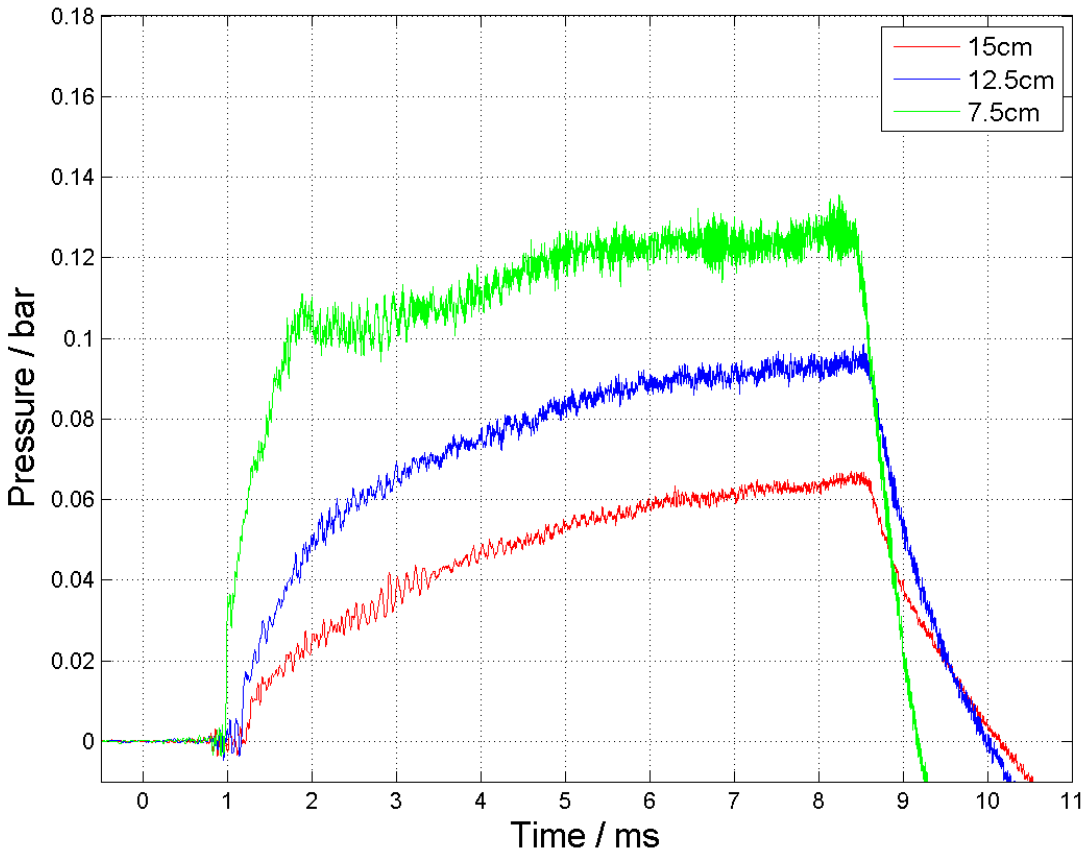


Shock Tube



Diaphragm	Burst pressure [bar]	M_s	20 kg TNT [2]
50 μm Mylar [®]	4.39 ± 0.05	1.31 ± 0.01	9.0 m
23 μm Mylar [®]	2.12 ± 0.03	1.26 ± 0.01	10.8 m
40 μm Al	1.43 ± 0.01	1.20 ± 0.01	12.6 m

- Whole driver tube \rightarrow full-volume
- Blanking flange, 10% charging length \rightarrow small-volume



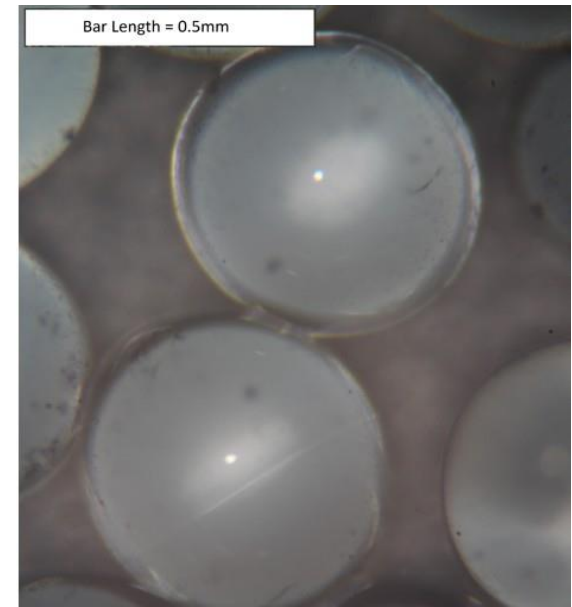
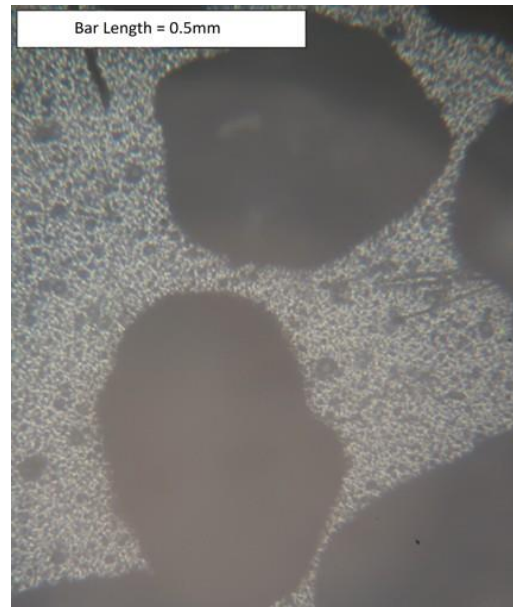
Dry and Dampened Beds

Dampened Beds

Material	Quoted Size
Small Sand	300–600 μm
Large Sand	1.18–2.36mm
Small soda lime glass spheres	400–600 μm
Large soda lime glass spheres	1.5 \pm 0.03

small sand & small spheres

white bar= 0.5 mm



Material	Permeability (mm^2)
Small Sand	$1.85(\pm 0.19) \times 10^{-5}$
Large Sand	$1.13(\pm 0.02) \times 10^{-3}$
Small Spheres	$7.14(\pm 0.01) \times 10^{-5}$
Large Spheres	$1.99(\pm 0.01) \times 10^{-3}$

Porosity : 0.27 Sand / 0.38 Spheres

Roundness*: sand = 0.45 / spheres = 1.0

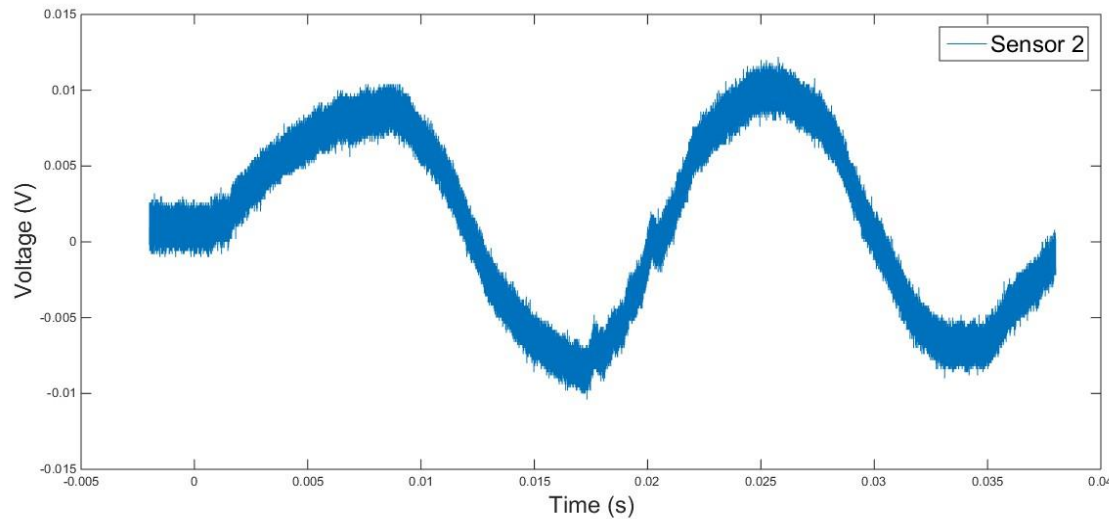
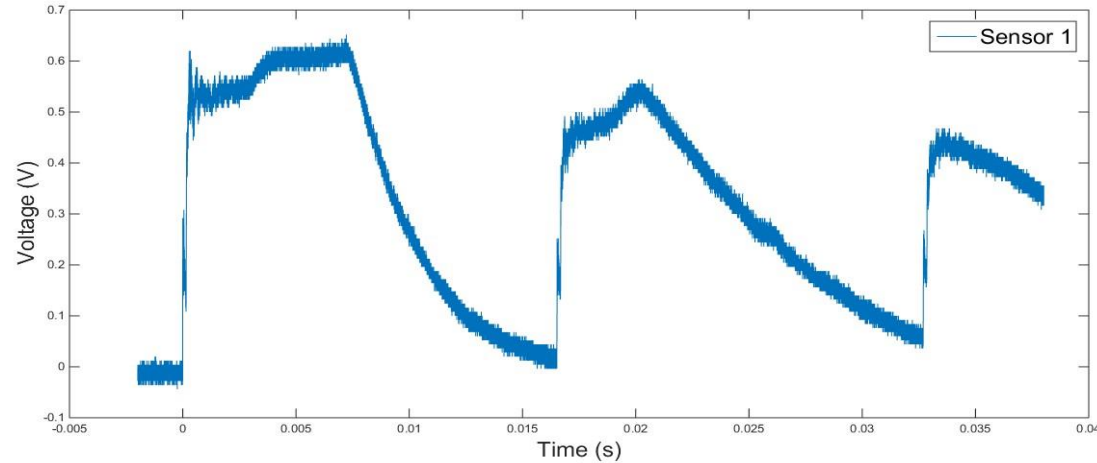
Porosity = fraction of void

Permeability = ability of a fluid to pass through it

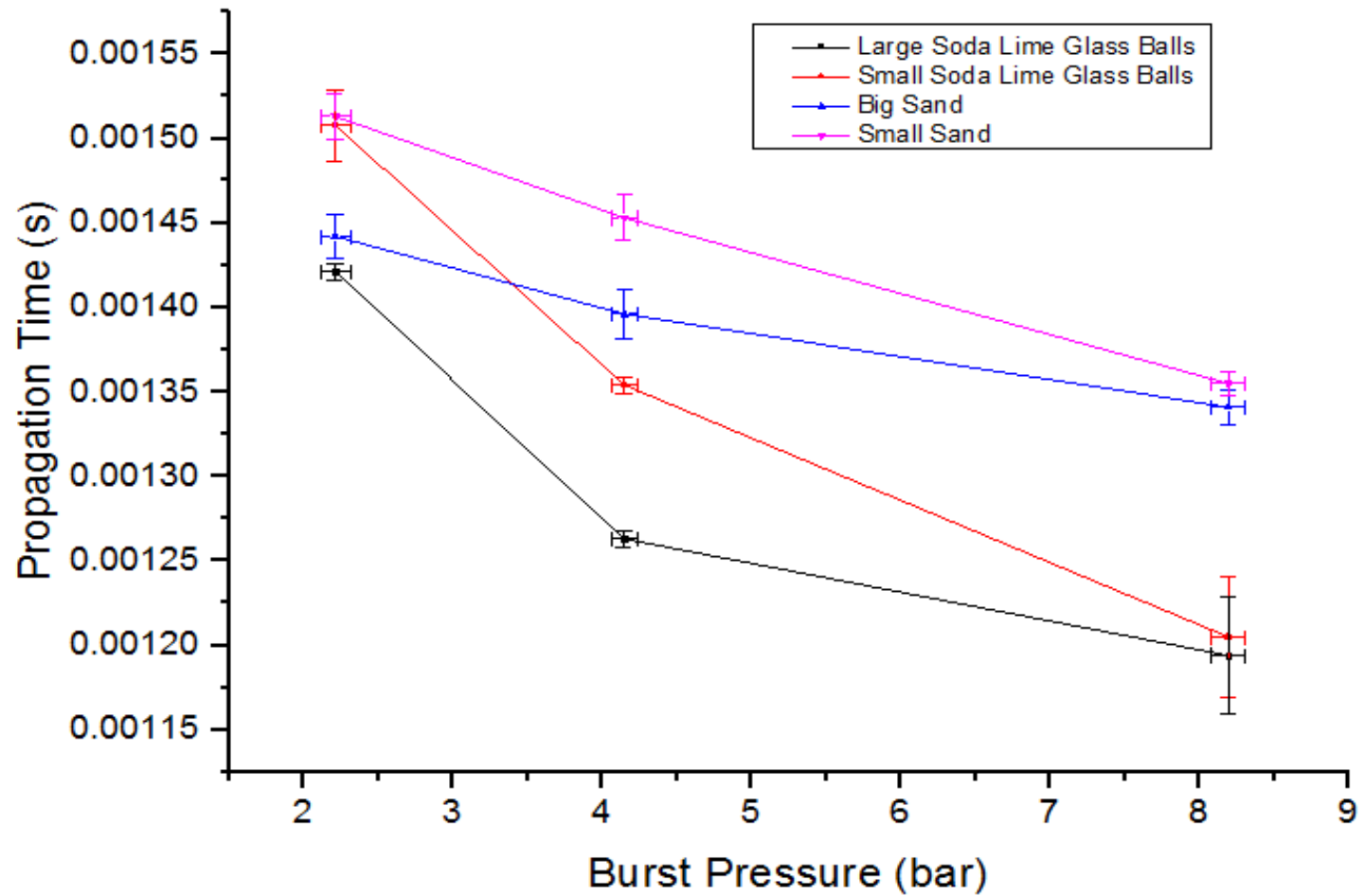
*RP Jensen *et al.*, Effect of particle shape on interface behavior of simulated granular materials. *International Journal of Geomechanics*, 1(1):1-19, 2001.

Input and Output Pulses

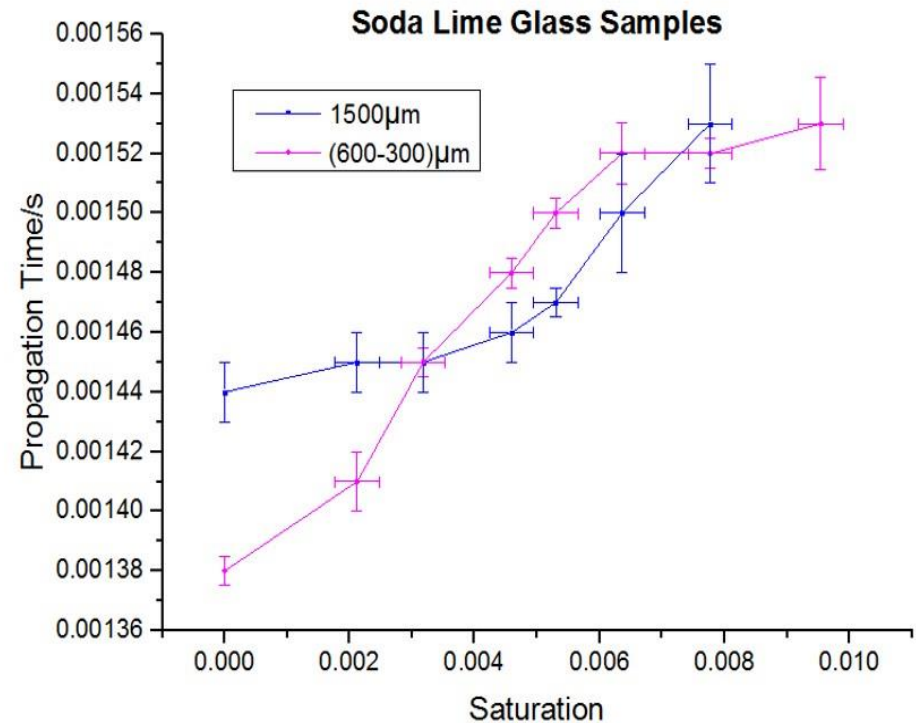
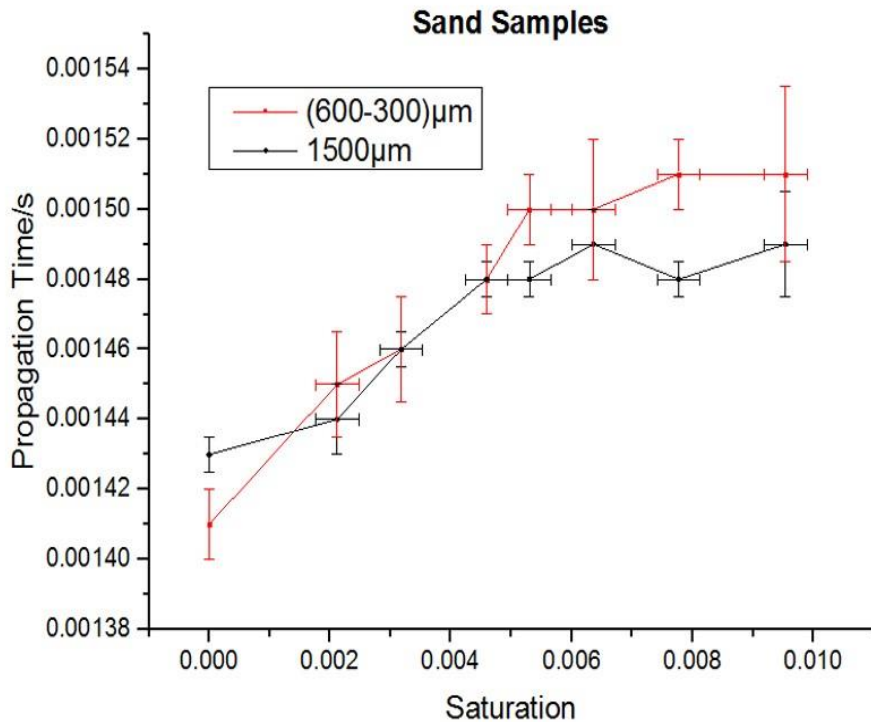
10 cm Bed
Small Sand



Propagation Time / Pressure (Dry)

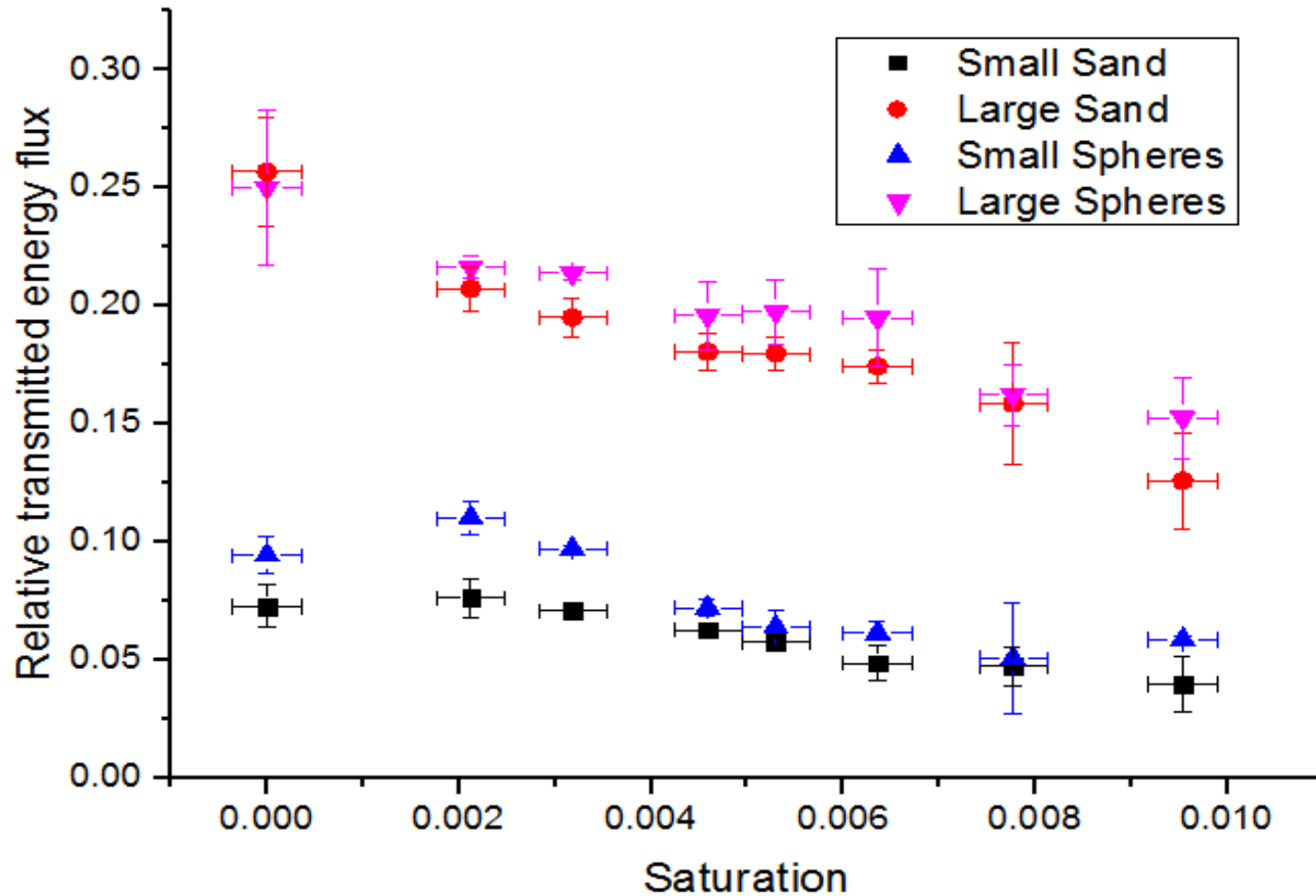


Propagation Time v Saturation



10 cm long granular bed

Energy Transmittance / Saturation



- **Grain size has an effect, more marked at low pressures**
- **Porosity has an effect**
- **Grain morphology seems to dominate at high pressures**
- **Small additions of water / oil etc has a marked effect on the system.**

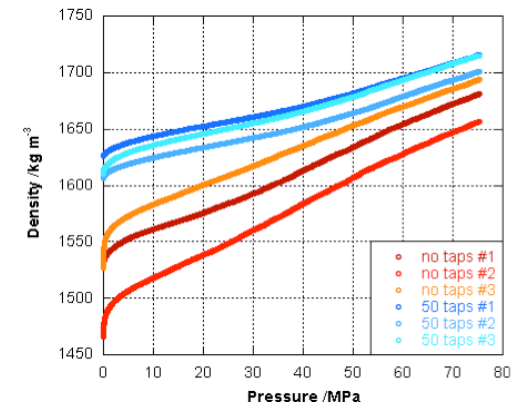
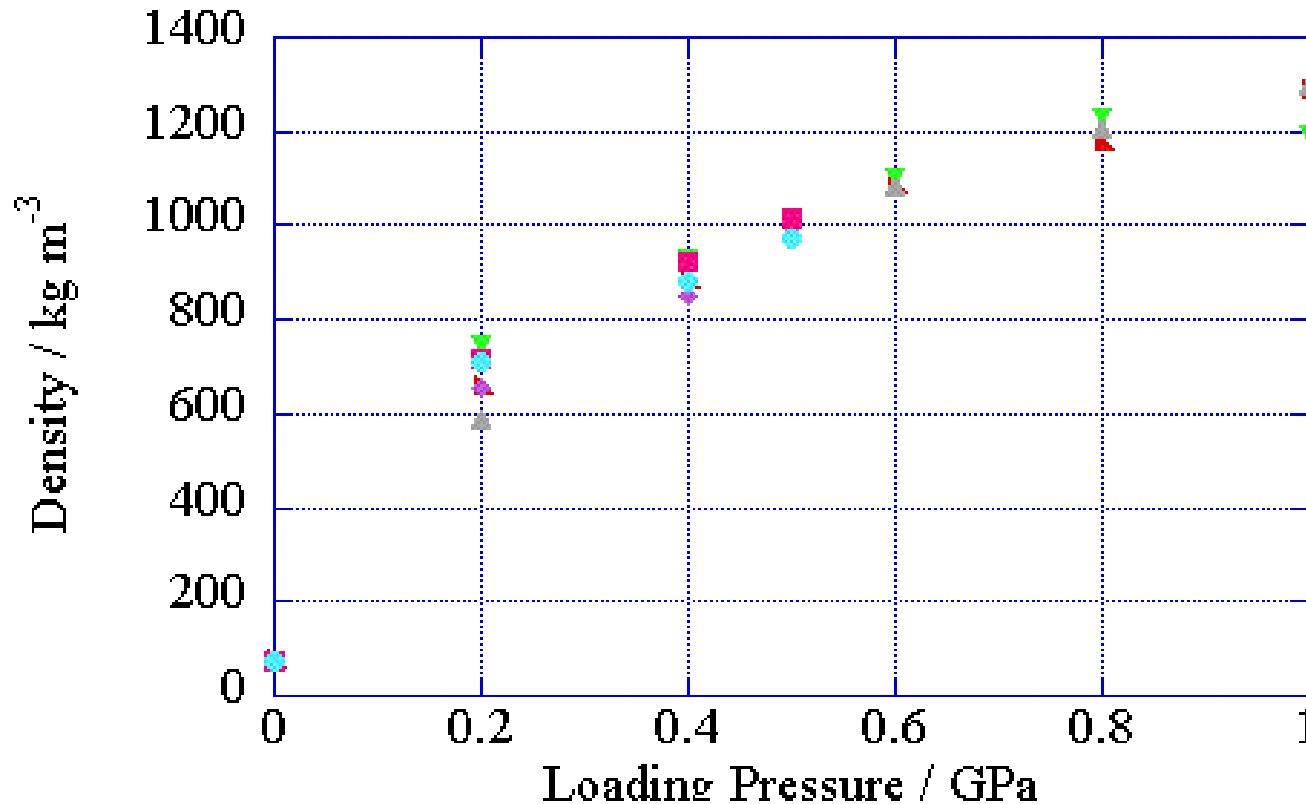
Other Effects

Does the shock wave obey 'simple' Rankine-Hugoniot relationships?

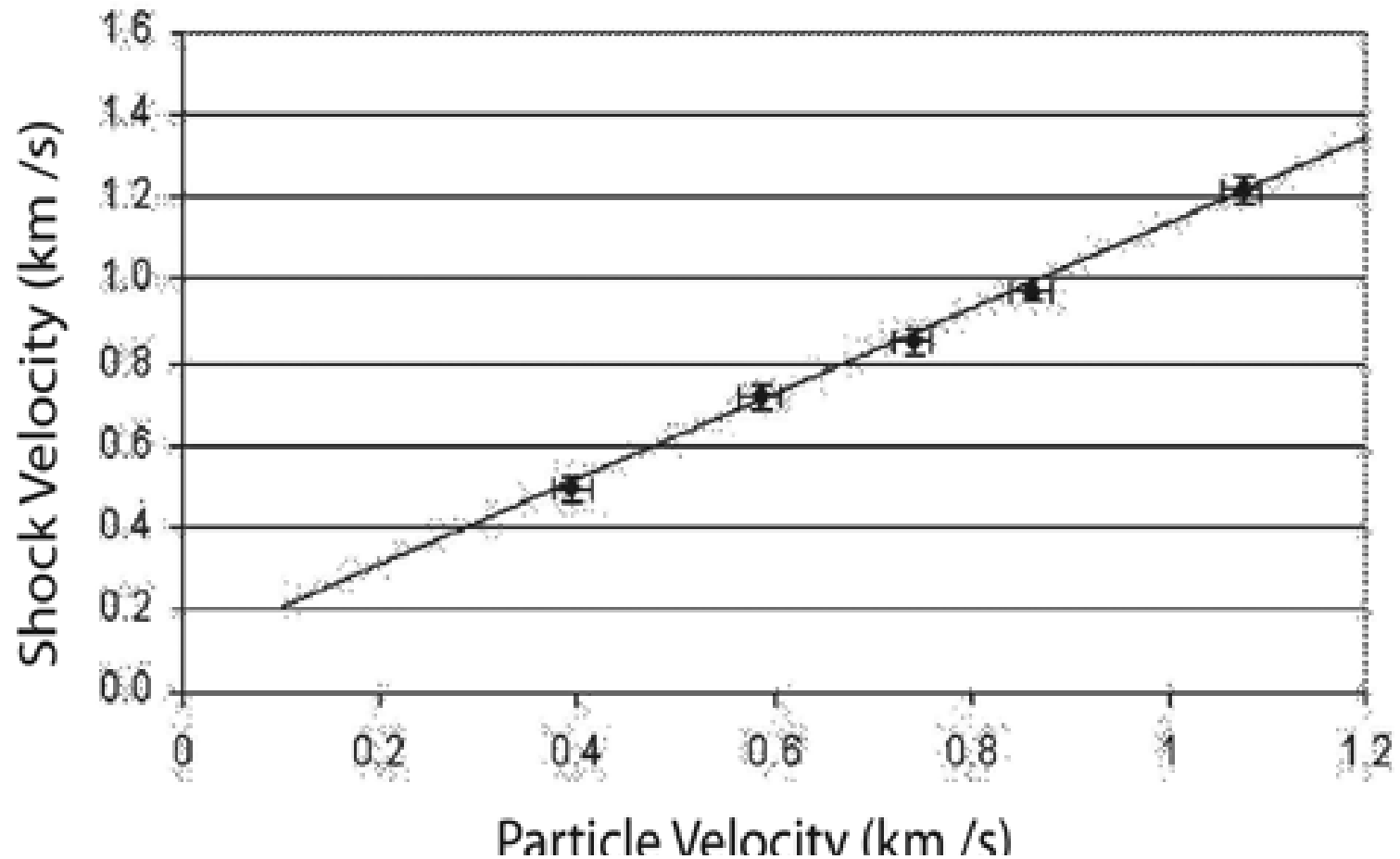
What is the sound speed in sand (it is well known it is frequency dependant)

Extreme 5% TMD Low Density Silica Dust

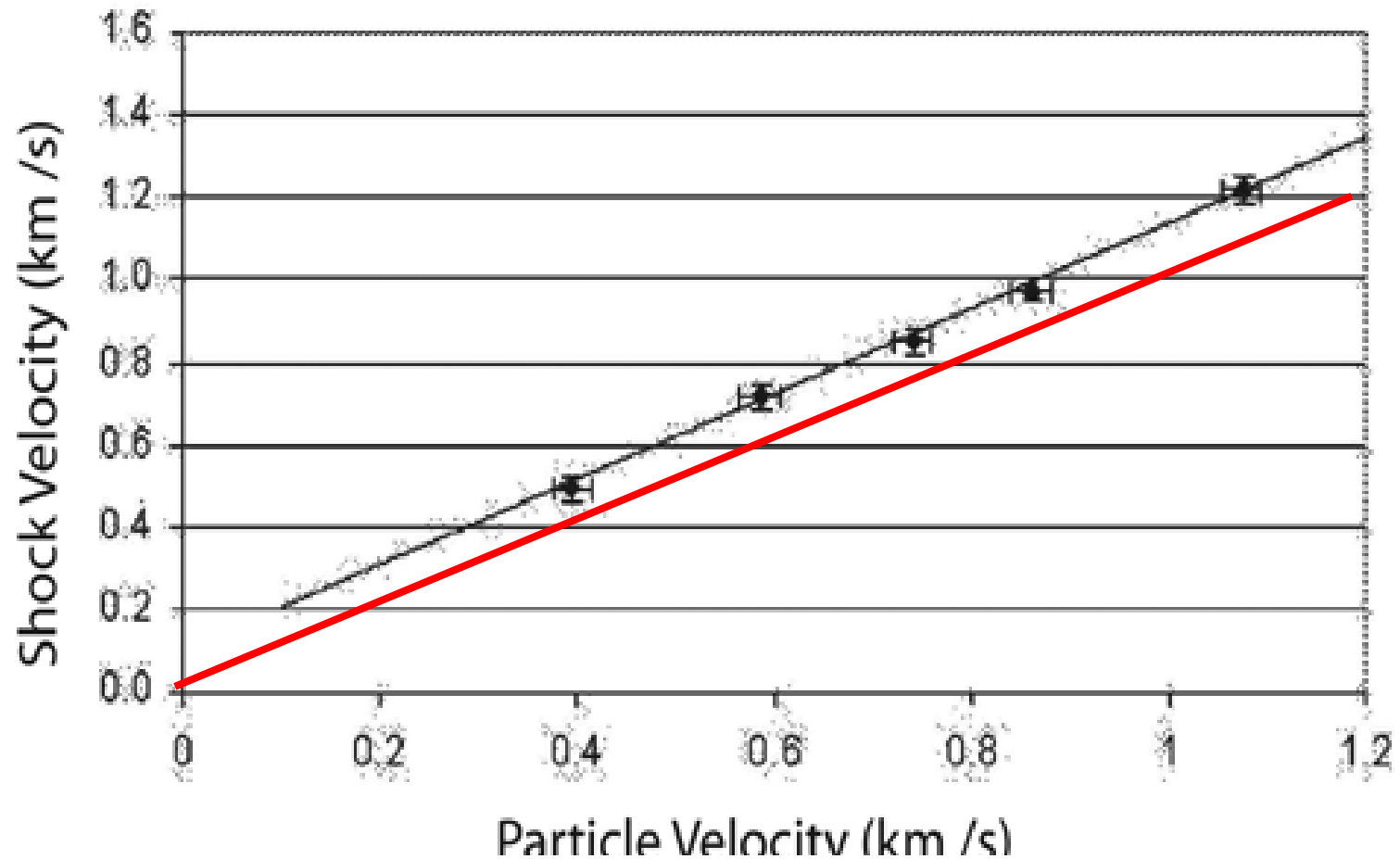
Low-rate



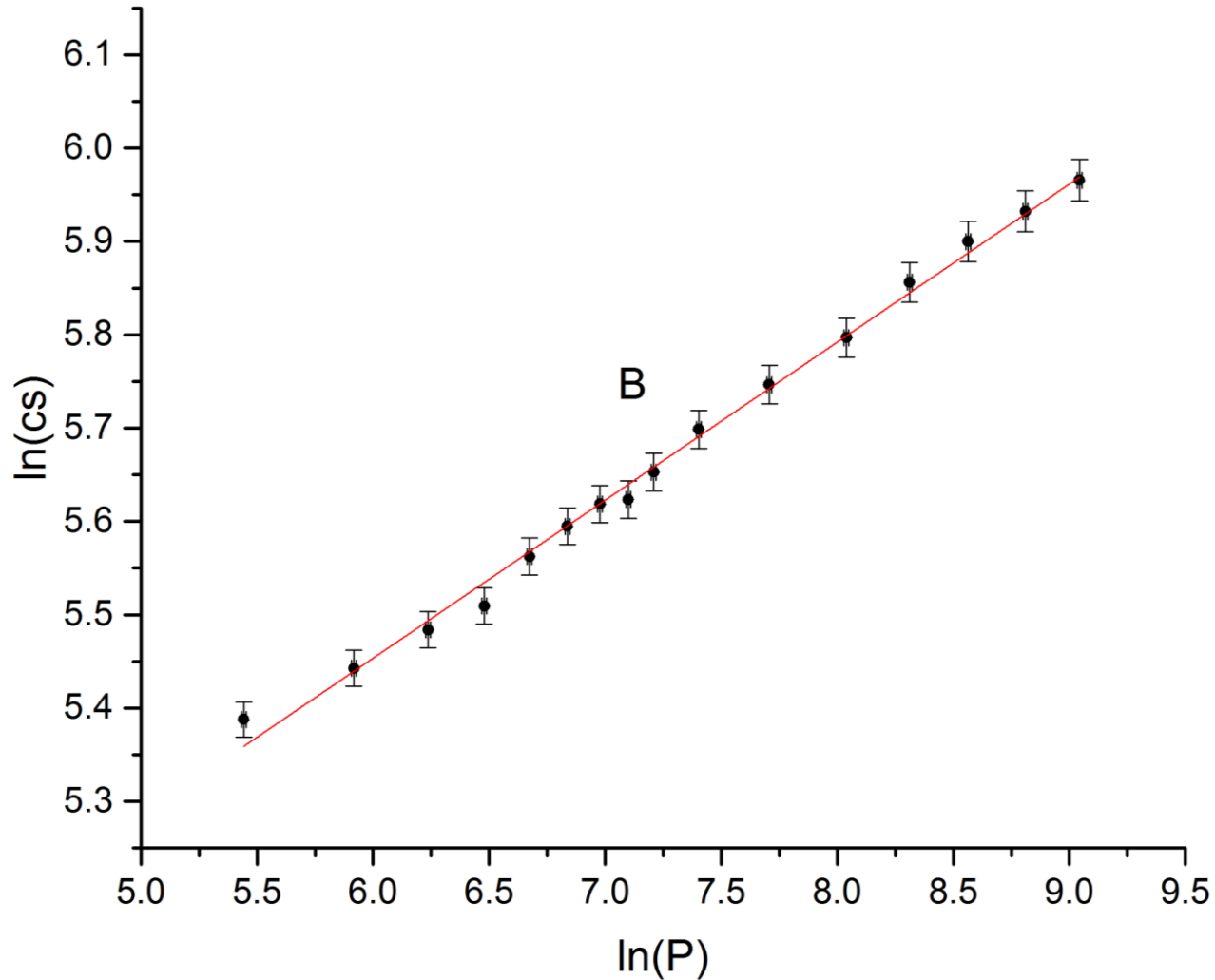
“Hugoniot”



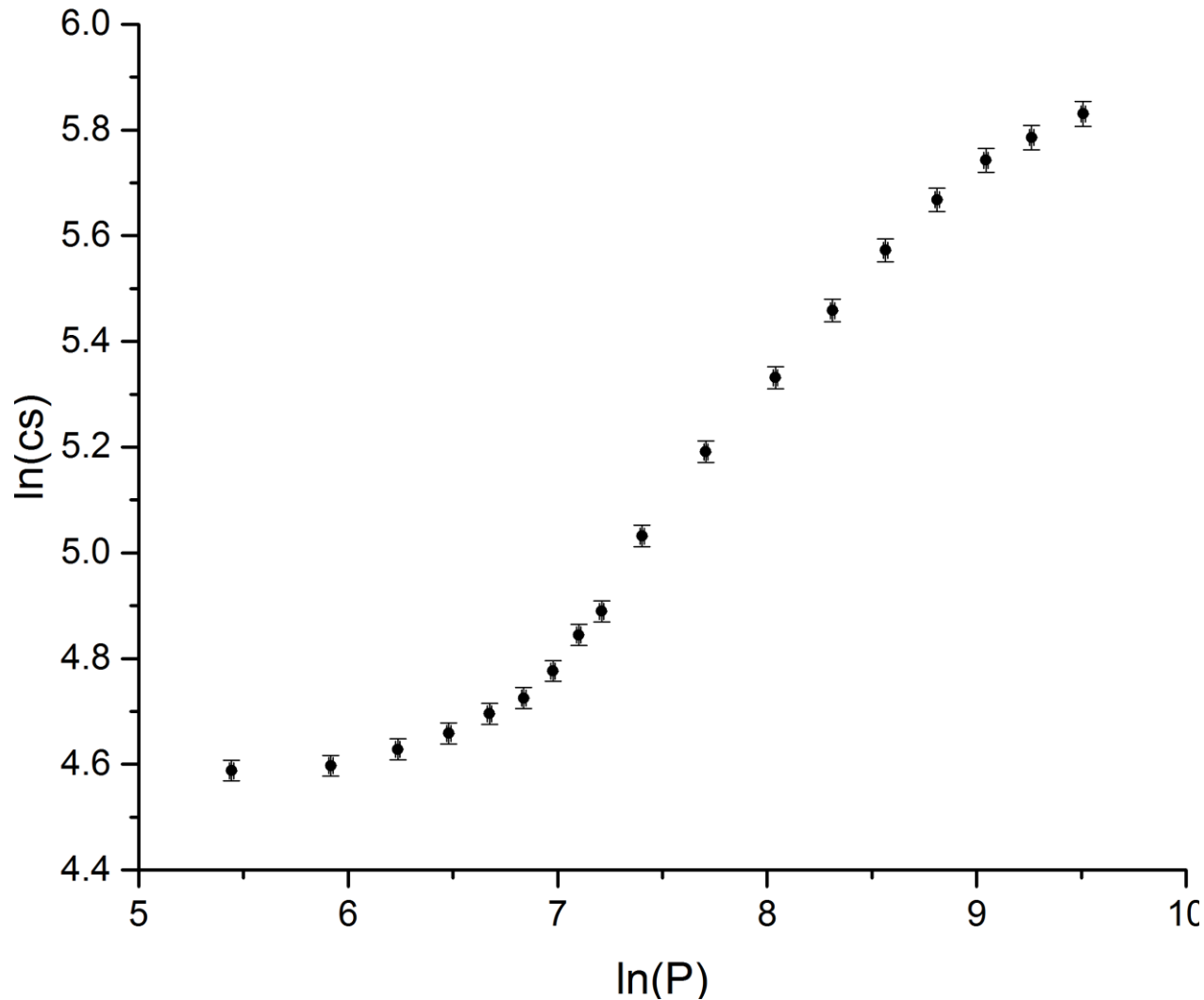
Hugoniot v. Compaction Line



Sound Speed - 2 mm Glass Spheres



Simple Property – Sand - Sound Speed



Need to define the starting conditions

What is the required output?

Physical Understanding (science-engineering driven)

Approximate Behaviour (application driven)

Natural Material

Constructed Material

Many ways of doing this, optimally - something simple to apply/ define

Particle Size Distribution

Material Type

Morphology

Contact Points

Before fracture / compaction etc.

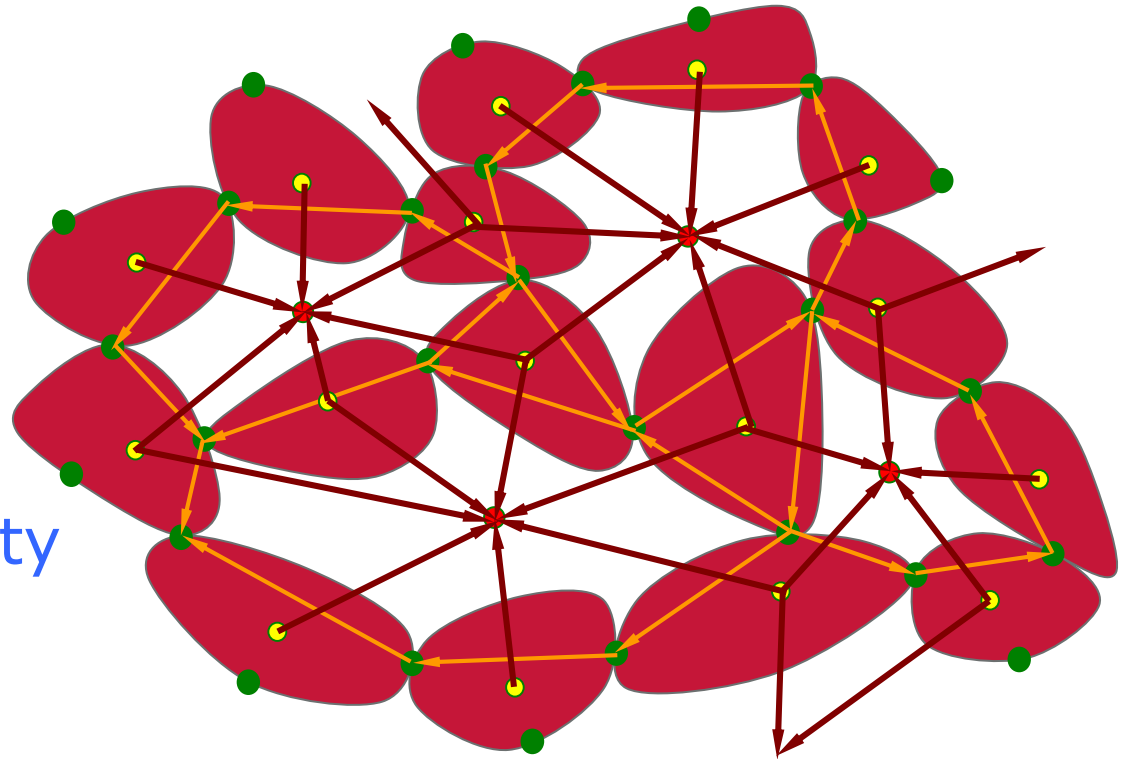
Parameters to
determine

Connectivity
Particle Size

Stability v Instability

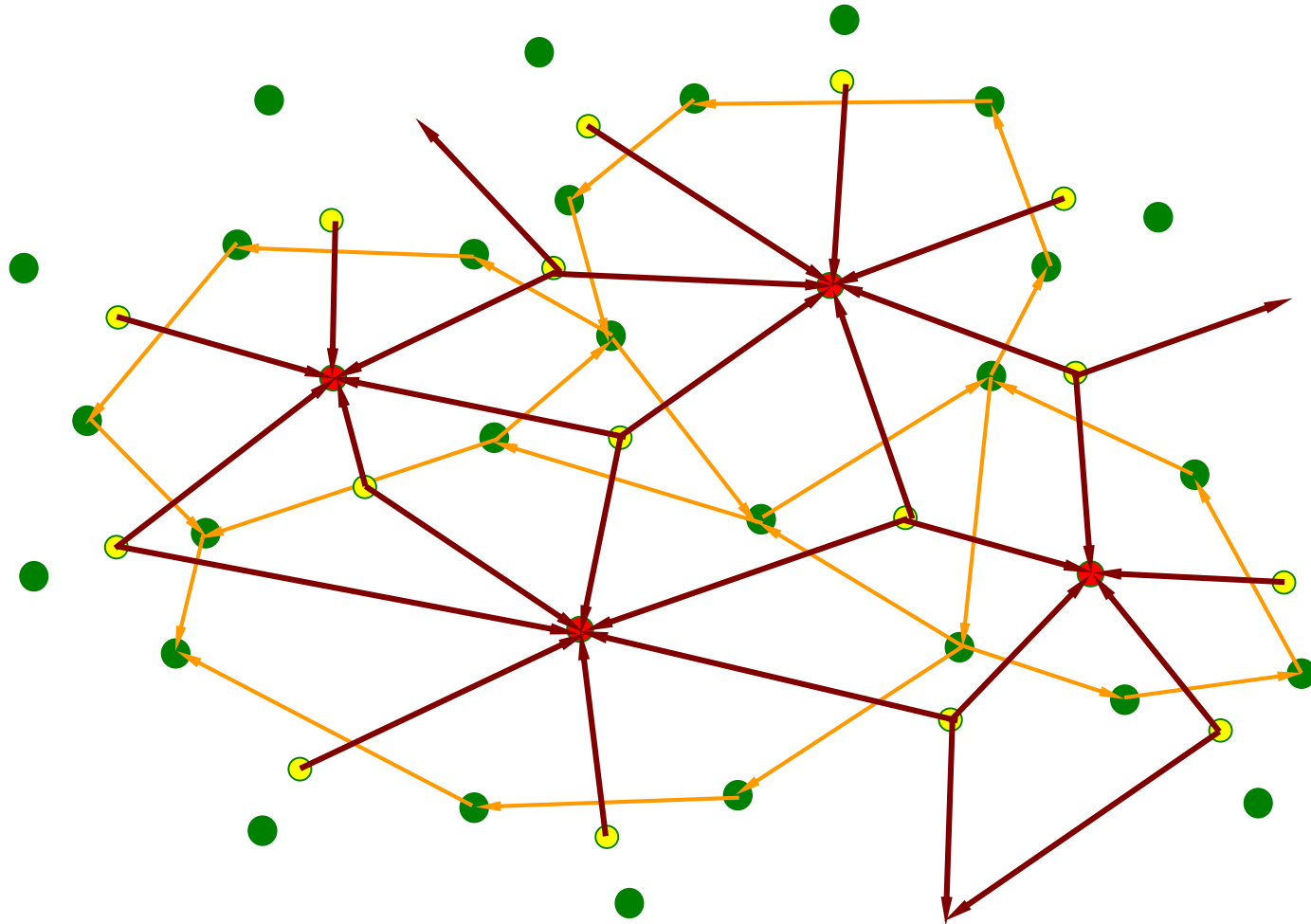
'Rattlers'

Grain Rotation



1. RB & SFE, Phys. Rev. Lett. 90, 114303-114306 (2003);
2. RCB & RB, Phys. Rev. Lett., 88, 115505-115508 (2002))
3. RB & SFE, Eur. Phys. J. E 19 , 23-30 (2006)
4. RB, SFE & SMW, Chapter on: *Granular systems*, in *The Oxford Handbook of Soft Condensed Matter*, Eds. E.M. Terentjev and D.A. Weitz, (Oxford University Press, Oxford, UK, 2015)

Quadron Tessalation



Conclusion

- **Many phenomena are partially understood (many models)**
- **Strain rate dependence is complex across the strain rates**
- **Properties within a material class are reproducible**
- **Start Conditions are important**

- **Use of Synchrotron-based studies to look in depth at high-rate compaction**